Grade 7/8 Math Circles

October 28, 2020

Propositions and Control Flow - Problem Set

- 1. Find the truth valuation for each of the given propositions if P is false, Q is true, and R is true.
 - (a) $(P \wedge Q) \vee (\neg R)$

- (c) $P \vee (R \wedge Q)$
- (a) $(P \wedge Q) \vee (\neg R)$ (b) $(Q \wedge (\neg P)) \wedge (R \wedge P)$ (c) $P \vee (R \wedge Q)$ (d) $(P \wedge (Q \vee (R \wedge (\neg P)))) \vee (Q \wedge (P \vee R))$
- 2. Find a proposition that is only true when either P and Q are both true or P is not true and R is true.
- 3. Find a proposition with P and Q that always has a true truth value (no matter the truth valuation).
- 4. Find a proposition with P and Q that always has a false truth value.
- 5. Draw the truth tables for the following propositions.

- $\begin{array}{ll} \text{(a)} & (P \wedge Q) \wedge (\neg P) \\ \text{(b)} & P \wedge (Q \vee (R \vee (\neg Q))) \\ \end{array} \\ \text{(c)} & (P \wedge R) \vee (Q \wedge \neg (Q \wedge P)) \\ \text{(d)} & ((P \vee Q) \vee (R \wedge (\neg P))) \vee (\neg Q) \\ \end{array}$
- 6. Write a boolean expression that can be used to determine if both x is less than 5 and y is 6.
- 7. Write a program that will print True if x is between or equal to y and z and x is not a multiple of 5. Assume that y is smaller than z.
- 8. Write a program that will print all the numbers between, but not equal to, y and zthat are not multiples of 2, but are multiples of 3. Assume you do not know which of y and z are smaller.
- 9. Write a program that, given three numbers, a, b and c, finds the smallest, greatest and middle number. Assume none of the numbers are equal.
- 10. Write a program that does something interesting. This could be helping to solve a math problem, a short game or anything you want to code. Share your code on Piazza!