

Le CENTRE d'ÉDUCATION en  
MATHÉMATIQUES et en INFORMATIQUE

# Problème de la semaine

## Problèmes et solutions

### 2021 - 2022

(solutions disponibles en anglais seulement)

## Problème A (3<sup>e</sup>/4<sup>e</sup> année)

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### Thèmes

(Cliquer sur le nom du thème ci-dessous pour sauter à cette section.)

**Sens du nombre (N)**

**Géométrie et mesure (G)**

**Algèbre (A)**

**Gestion des données (D)**

**Raisonnement informatiques (C)**

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Les problèmes dans ce livret sont organisés par thème.

Un problème peut apparaître dans plusieurs thèmes.

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# Sens du nombre (N)

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## Problème de la semaine

### Problème A

#### Calcul de nettoyage

Un homme de ménage est chargé de nettoyer toutes les chambres d'un étage d'un hôtel. L'étage compte 16 chambres régulières et 5 suites. Chaque chambre régulière peut être nettoyée en 20 minutes. Chaque suite peut être nettoyée en 30 minutes.

- (a) Combien de temps faut-il pour nettoyer toutes les chambres sur cet étage?
- (b) Si l'homme de ménage commence à nettoyer à 10 h du matin et qu'il ne prend pas de pause, à quelle heure aura-t-il terminé son travail?





## Problem of the Week Problem A and Solution Cleaning Calculation

### Problem

A housekeeper is responsible for cleaning all the rooms on one floor of a hotel. The floor has 16 regular rooms and 5 suites. Regular rooms take 20 minutes each to clean. Suites take 30 minutes each to clean.

- (a) How long does it take to clean all the rooms on the floor of the hotel?
- (b) If the housekeeper starts cleaning at 10:00 a.m. and does not take a break, at what time is the job finished?

### Solution

- (a) We can calculate the time it takes to clean the regular rooms by skip counting by 20:

20, 40, 60, 80, 100, 120, 140, 160, 180, 200, 220, 240, 260, 280, 300, 320

We see that it takes a total of 320 minutes to clean the regular rooms.

We can calculate the time it takes to clean the suites by skip counting by 30:

30, 60, 90, 120, 150

We see that it takes a total of 150 minutes to clean the suites. We add these two numbers together to see that it takes a total of  $320 + 150 = 470$  minutes to clean the entire floor.

From this total number of minutes, we could calculate the result in hours and minutes.

However, we could also recognize that when skip counting by 20, we get to 60 minutes after three 20-minute intervals. This means it takes an hour to clean three regular rooms.

We could count a bit differently:

20 min, 40 min, 1 hour, 80 min, 100 min, 2 hours, 140 min, 160 min, 3 hours, 200 min,  
220 min, 4 hours, 260 min, 280 mins, 5 hours, 320 mins

We can see that 320 minutes is equal to 5 hours and 20 minutes.

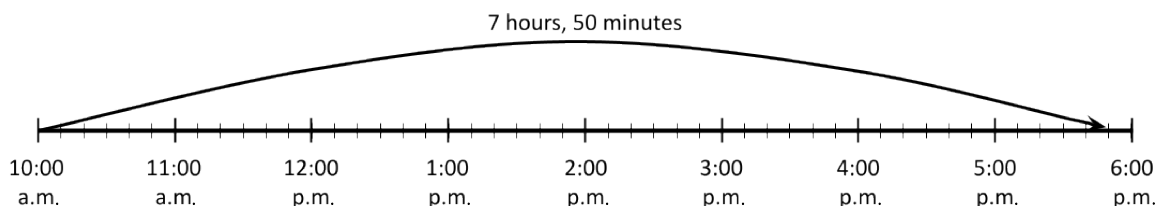
Similarly, we get to 60 minutes after two 30-minute intervals. With similar counting we see that 150 minutes is equal to 2 hours and 30 minutes.

Now we can find the total time taken as:

$$5 \text{ hours} + 2 \text{ hours} + 20 \text{ minutes} + 30 \text{ minutes}$$

which is equal to 7 hours and 50 minutes.

- (b) We can use a timeline to determine the time that is 7 hours and 50 minutes after 10:00 a.m.



Therefore, the housekeeper will finish the job at 5:50 p.m.



## Teacher's Notes

Although we often think of *rates* as being related to distance and time, we can describe this problem in terms of rates. The units we use when describing rates is:

$$(\text{some quantity})/(\text{some unit of time})$$

For example, a car's speed may be measured in *km/hr* or a computer's download speed may be measured in *MBits/sec*.

When working with rates involving distance and time, we can consider this formula that shows the relationship between *rate*, *distance*, and *time*:

$$\text{rate} = \frac{\text{distance}}{\text{time}}$$

Given any two of the values, we can use the formula to calculate the third. For example, if we know the *rate* and *time*, we can calculate the distance. Often we rearrange the formula to make it easier to calculate the missing value, where the missing value is isolated on one side of the equals sign.

$$\text{rate} \times \text{time} = \text{distance} \quad \text{and} \quad \text{time} = \frac{\text{distance}}{\text{rate}}$$

For this problem, we can consider the following formula for the rate of cleaning:

$$\text{rate} = \frac{\text{rooms}}{\text{time}}$$

For regular rooms, we know the rate is  $\frac{1 \text{ room}}{20 \text{ min}}$  and the number of rooms is 16.

We can rearrange the formula to isolate the time:

$$\text{time} = \frac{\text{rooms}}{\text{rate}}$$

Now we can substitute the actual numbers into this formula:

$$\text{time} = \frac{16 \text{ rooms}}{\frac{1 \text{ room}}{20 \text{ mins}}}$$

To calculate this result we must divide by a fraction, which we can do by inverting the fraction and multiplying like this:

$$\begin{aligned} \text{time} &= 16 \cancel{\text{rooms}} \times \frac{20 \text{ mins}}{1 \cancel{\text{room}}} \\ \text{time} &= 320 \text{ mins} \end{aligned}$$



## Problème de la semaine

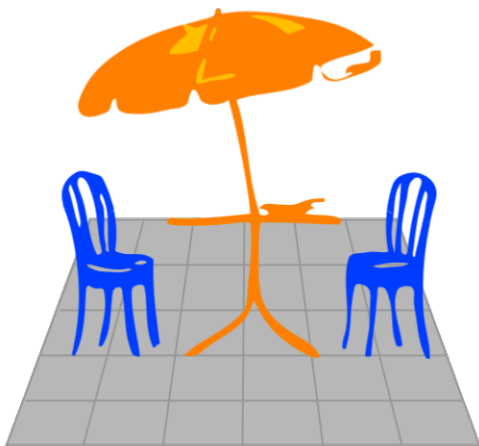
### Problème A

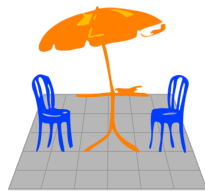
#### Conception de terrasse

Jody et Jillian veulent construire une terrasse derrière leur maison. Ils comptent utiliser des pierres carrées dont les côtés ont une longueur de 50 cm. Ils ont, en tout, 75 pierres carrées disponibles.

Pour construire la terrasse, ils placent les pierres carrées de manière à ce que deux pierres côte à côte se touchent et que leurs côtés soient parfaitement alignés. Ils n'utiliseront que des pierres carrées entières et ils veulent que toute la terrasse soit entièrement recouverte de pierres.

- (a) S'ils voulaient que leur terrasse ait la forme d'un carré, quelles sont les dimensions de la plus grande terrasse qu'ils pourraient construire?
- (b) S'ils voulaient que leur terrasse ait la forme d'un rectangle dont la longueur d'un côté est le double de la longueur de l'autre côté, quelles sont les dimensions de la plus grande terrasse qu'ils pourraient construire?





## Problem of the Week

### Problem A and Solution

### Patio Planning

#### Problem

Jody and Jillian are building a patio beside their house. They have square patio stones that have sides with a length of 50 cm. They have a total 75 patio stones available.

To build the patio, they place the patio stones so that two stones next to each other are touching and their sides are lined up exactly. They will only use whole patio stones and they want the entire patio covered in stones.

- (a) If they want to have their patio in the shape of a square, what are the dimensions of the largest possible patio they can build?
- (b) If they want to build a patio in the shape of a rectangle where the length of one side is twice as long as the length of the other side, what are the dimensions of the largest patio they can build?

#### Solution

- (a) The following table shows the possible sizes of the patio if the patio is in the shape of a square.

Length	Width	Number of Stones Used
1	1	$1 \times 1 = 1$
2	2	$2 \times 2 = 4$
3	3	$3 \times 3 = 9$
4	4	$4 \times 4 = 16$
5	5	$5 \times 5 = 25$
6	6	$6 \times 6 = 36$
7	7	$7 \times 7 = 49$
8	8	$8 \times 8 = 64$
9	9	$9 \times 9 = 81$

Since there are only 75 patio stones available, the biggest square patio that Jody and Jillian can build is 8 patio stones long by 8 patio stones wide. Since each square patio stone has sides with length 50 cm, then 8 stones in a line have a length of  $8 \times 50 = 400$  cm or 4 metres. So the largest square patio made out of 75 or fewer patio stones has dimensions 4 meters long by 4 metres wide.



- (b) To investigate a patio that has one side that is twice as long as the other side, we can name the shorter side Length and the longer side Width. The following table shows the possible sizes of the patio.

Length	Width	Number of Stones Used
1	2	$1 \times 2 = 2$
2	4	$2 \times 4 = 8$
3	6	$3 \times 6 = 18$
4	8	$4 \times 8 = 32$
5	10	$5 \times 10 = 50$
6	12	$6 \times 12 = 72$
7	14	$7 \times 14 = 98$

Since we only have 75 patio stones, the biggest patio Jody and Jillian can build that has one side twice as long as the other side is a rectangle that is 6 patio stones long by 12 patio stones wide. Since each square patio stone has sides with length 50 cm, then 6 stones in a line have a length of  $6 \times 50 = 300$  cm or 3 metres, and 12 stones in a line have a length of  $12 \times 50 = 600$  cm or 6 metres. So the largest patio with one side twice as long as the other side and made out of 75 or fewer patio stones, has dimensions 3 metres by 6 metres.





## Problème de la semaine

### Problème A

#### Pas de cents

Au Canada, on exprime habituellement les prix en dollars et en cents. Un prix peut être exprimé sous la forme d'un nombre décimal; le montant en dollars paraissant avant la virgule et le montant en cents après la virgule.

Zahra tient un magasin qui a décidé de supprimer les cents dans ses prix. Cela signifie que tous les nouveaux prix seront arrondis au dollar près de manière que chaque prix se termine par ,00.

Voici quelques-uns des articles en vente dans son magasin ainsi que leurs prix initiaux:

Article	Prix
Patins à roulettes	54,59 \$
Casque	25,25 \$
Protège-coudes	15,88 \$
Planche à roulettes	75,75 \$
Vélo	105,32 \$
Cadenas de vélo	25,44 \$
Protège-poignets	20,99 \$

- Détermine le nouveau prix de chaque article.
- Si Zahra vend un article de chaque type, gagnera-t-elle plus ou moins d'argent qu'avant? Justifie ta réponse.





## Problem of the Week

### Problem A and Solution

#### Non-cents

#### Problem

Canadian prices are normally in dollars and cents, with the dollar amount appearing before the decimal point and the cents amount appearing after the decimal point.

Zahra has a store that has decided to get rid of cents in their pricing. This means that all new prices will be rounded to the nearest dollar amount so that each price ends with .00.

These are some of the items in her store as well as their original prices:

Item	Price
Rollerblades	\$54.59
Helmet	\$25.25
Elbow Pads	\$15.88
Skateboard	\$75.75
Bicycle	\$105.32
Bike Lock	\$25.44
Wrist Guards	\$20.99

- (a) What will the new price of each item be?
- (b) If she sells one of each type of item, will Zahra be making more money or less money than before? Justify your answer.

#### Solution

- (a) Here are the new prices rounded to the nearest dollar:

Item	New Price
Rollerblades	\$55.00 (rounded up)
Helmet	\$25.00 (rounded down)
Elbow Pads	\$16.00 (rounded up)
Skateboard	\$76.00 (rounded up)
Bicycle	\$105.00 (rounded down)
Bike Lock	\$25.00 (rounded down)
Wrist Guards	\$21.00 (rounded up)



- (b) There are many ways to determine the impact of the new prices. One option is to find the totals of the original prices and the new prices, and then calculate the difference of those totals. To keep things a bit simpler, since the tens and hundreds place values have not changed, then we can ignore the tens and hundreds place values of the prices.

Original total (ignoring the tens and hundreds place values):

$$4.59 + 5.25 + 5.88 + 5.75 + 5.32 + 5.44 + 0.99 = \$33.22$$

New total (ignoring the tens and hundreds place values):

$$5 + 5 + 6 + 6 + 5 + 5 + 1 = \$33$$

We see that the new total is 22 cents less than the original total. Therefore, Zahra will be making less money with the new pricing.

Another way to determine the difference is to find out how much more or less the new individual prices will be compared to the old prices. These amounts are all in cents. For example:

- The new rollerblades price is 41 cents more than the original price since we rounded up and  $59 + 41 = 100$ .
- The new helmet price is 25 cents less than the original price since we rounded down.

Zahra will make more money on the items where the prices were rounded up, and less on the items that were rounded down.

More money:  $41 + 12 + 25 + 1 = 79$  cents

Less money:  $25 + 32 + 44 = 101$  cents

The “less money” amount is greater than the “more money” amount. Overall, Zahra will make  $101 - 79 = 22$  cents less than before with the new pricing.



## Problème de la semaine

### Problème A

#### Quel nombre suis-je?

Je suis un nombre de cinq chiffres composé des chiffres 0, 3, 4, 6 et 9 tel que:

- Le chiffre **4** occupe une position dont la valeur est 10 fois celle de la position occupée par le chiffre **9** et 100 fois celle de la position occupée par le chiffre **0**.
- Le chiffre **3** occupe une position dont la valeur est 100 fois celle de la position occupée par le chiffre **9**.
- Le chiffre **0** occupe une position dont la valeur est 10 fois celle de la position occupée par le chiffre **6**.

Quel nombre suis-je?





## Problem of the Week Problem A and Solution What Number Am I?

### Problem

I am a five-digit number made of the digits 0, 3, 4, 6, and 9. In my number, the following are true.

- The digit **4** is in a position whose place value is 10 times the place value of the position of the digit **9** and 100 times the place value of the position of the digit **0**.
- The digit **3** is in a position whose place value is 100 times the place value of the position of the digit **9**.
- The digit **0** is in a position whose place value is 10 times the place value of the position of the digit **6**.

What number am I?

### Solution

The positions in a five-digit number are: ones (units), tens, hundreds, thousands, and ten thousands.

Since the 4 is in a position whose place value is 10 and 100 times the place value of other positions, the 4 cannot be in the ones or tens position.

Since the 3 is in a position whose place value is 100 times the place value of another position, the 3 cannot be in the ones or tens position.

Since the 0 is in a position whose place value is 10 times the place value of another position, the 0 cannot be in the ones position.

So the ones position must contain either the 9 or the 6.

Let's assume that the 9 is in the ones position. Based on the first clue, the 4 must be in the tens position since  $10 \times 1 = 10$ . However, we have already stated that the 4 cannot be in the ones or tens position. So we cannot put the 9 in the ones position.

Therefore, we can conclude that the 6 is in the ones position. Based on the third clue, the 0 must be in the tens position since  $10 \times 1 = 10$ . Knowing that the 0 is in the tens position, we can use the first clue to conclude that the 4 must be in the thousands position, since  $100 \times 10 = 1000$ . Also, the 9 must be in the hundreds position, since  $10 \times 100 = 1000$ . Now the only position that is left, the ten thousands position, must contain the only digit left which is the 3. This is consistent with the second clue since  $100 \times 100 = 10\,000$ .

Therefore, the number must be 34906.



## Problème de la semaine

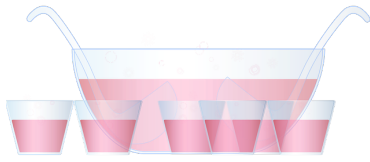
### Problème A

#### Un punch parfait

Su prépare du punch pour ses camarades. Elle veut mélanger 3 L de jus d'orange, 1 L de boisson gazeuse,  $\frac{1}{2}$  L de jus de raisin et 300 mL de jus de canneberge dans un bol à punch.

- (a) Pour prévenir les dégâts, Su prévoit d'utiliser un bol à punch dont la capacité doit dépasser d'au moins 200 mL le volume du liquide qu'il contiendra. Quelle est la plus petite capacité que devrait avoir son bol à punch?
- (b) Su a des verres qui peuvent contenir chacun 300 mL de punch. Combien de ces verres peut-elle remplir avec le punch qu'elle prépare?





## Problem of the Week

### Problem A and Solution

### Perfect Punch

#### Problem

Su is going to make punch for her friends. She wants to mix 3 L of orange juice, 1 L of pop,  $\frac{1}{2}$  L of grape juice, and 300 mL of cranberry juice in a punch bowl.

- To avoid spilling, Su plans to use a punch bowl with a capacity of at least 200 mL more than the liquid it holds. What is the smallest capacity that her punch bowl should have?
- Su has cups that can each hold 300 mL of punch. How many of these cups can she fill with the punch she makes?

#### Solution

- The smallest capacity of the punch bowl is the sum of the volumes of each liquid, plus the 200 mL of extra space to avoid spilling.

One way to calculate this would be to convert all the volumes to millilitres.

- 3 L = 3000 mL
- 1 L = 1000 mL
- $\frac{1}{2}$  L = 500 mL

So the minimum capacity is  $3000 + 1000 + 500 + 300 + 200 = 5000$  mL.

Alternatively, we might notice that the sum of the volume of cranberry juice and the extra room for spillage is:  $300 + 200 = 500$  mL or  $\frac{1}{2}$  L.

So the minimum capacity is  $3 + 1 + \frac{1}{2} + \frac{1}{2} = 5$  L.

- The volume of punch is  $3000 + 1000 + 500 + 300 = 4800$  mL.

We can use skip counting to figure out how many cups of punch Su can fill:

300, 600, 900, 1200, 1500, 1800, 2100, 2400, 2700, 3000, 3300, 3600, 3900, 4200, 4500, 4800

We can see from this that Su can fill 16 cups with punch.

Alternatively, we can calculate the number of cups of punch by dividing  $4800 \div 300 = 16$  cups.

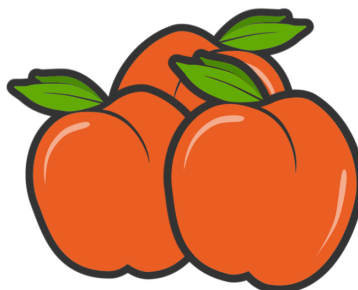


## Problème de la semaine

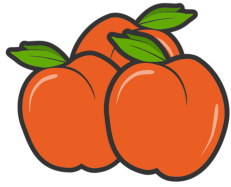
### Problème A

#### Des tartelettes savoureuses

Geneviève et Dima ont décidé de faire des tartelettes aux pêches. D'après leur recette, chaque tartelette requiert les trois quarts d'une pêche. Si elles ont acheté une douzaine de pêches, combien de tartelettes peuvent-elles préparer?







# Problem of the Week

## Problem A and Solution

### Tasty Tarts

#### Problem

Genevieve and Dima decided to make peach tarts. According to their recipe, each tart requires three-quarters of a peach. If they bought a dozen peaches, how many tarts can they make?

#### Solution

Here is one way to solve the problem. We can draw a diagram of a dozen peaches where each peach is divided into four quarters. Then we group three quarters together with a common label, corresponding to the tart that those quarters are used in. We continue to identify groups of three quarters over the dozen peaches. Finally, we count the number of groups we have identified.



From this diagram, we can see that Genevieve and Dima can make 16 tarts with a dozen peaches.



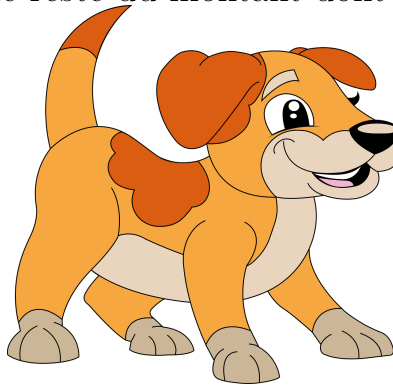
## Problème de la semaine

### Problème A

#### Adopter un chien

Robbie veut adopter un chien. Il décide de contribuer aux dépenses essentielles. Il veut faire un don de 60 \$ au refuge pour animaux d'où il pense adopter son chien. De plus, il compte participer à l'achat de la nourriture pour chiens à raison de 10 \$ par mois.

- (a) En tout, combien lui coûtera l'adoption et la nourriture pour chiens pendant la première année?
- (b) Robbie doit économiser le montant calculé dans la partie (a) avant d'adopter le chien. Il a 87 \$ dans sa tirelire. Il reçoit une allocation de 7 \$ chaque semaine pour avoir fait ses tâches ménagères. Combien de temps lui faudra-t-il pour gagner le reste du montant dont il a besoin?





## Problem of the Week

### Problem A and Solution

#### Puppy Plans

#### Problem

Robbie wants to get a puppy, so he decides to help pay the costs. He wants to donate \$60 to the animal shelter he gets the puppy from, and he needs to contribute \$10 every month to help buy the puppy's food.

- How much money does Robbie need to help pay the cost of getting the puppy and feeding the puppy in the first year?
- Robbie needs to save the money calculated in part (a) before getting the puppy. He has \$87 in his piggy bank. He earns a \$7 allowance every week for doing his chores. How long will it take Robbie to earn the rest of the money he needs?

#### Solution

- Since there are 12 months in a year and Robbie wants to contribute \$10 each month, he needs  $12 \times 10 = \$120$  for puppy food in the first year. Counting the shelter donation, Robbie needs  $\$60 + \$120 = \$180$  in total.
- We can make a table to calculate how long it will take for Robbie to save enough money to have at least \$180. He starts with \$87 and will increase his total by \$7 each week.

Week	Total Saved (in \$)
0	87
1	94
2	101
3	108
4	115
5	122
6	129
7	136
8	143
9	150
10	157
11	164
12	171
13	178
14	185

So it will take Robbie 14 weeks to earn enough money to help cover the shelter donation and the costs of feeding the puppy in the first year.

Alternatively, since Robbie has already saved \$87, he needs to earn  $\$180 - \$87 = \$93$  more. We calculate how long it will take to earn the remaining amount using division. Since  $93 \div 7 = 13$  with a remainder of 2, we round up to determine that it will take 14 weeks to earn the additional \$93 Robbie needs.



## Problème de la semaine

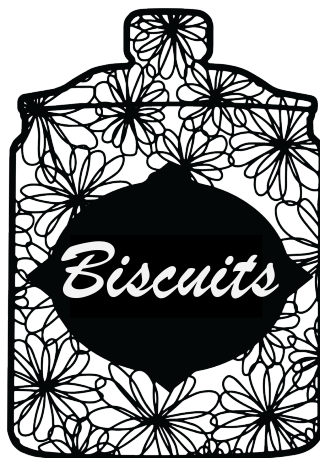
### Problème A

### Des biscuits!

Benoît, Jin, Manuel et Sarah ont partagé un paquet de 30 biscuits. Après plusieurs jours, tous les biscuits du paquet avaient été mangés par ces quatre amis et chacun d'eux n'a mangé que des biscuits entiers. Benoît a noté les observations suivantes:

- Sarah a mangé deux fois plus de biscuits que Jin.
- Manuel a mangé les deux tiers du nombre de biscuits que Sarah a mangé.
- Benoît a mangé moitié moins de biscuits que Manuel.

- (a) Qui a mangé le plus de biscuits? Justifie ta réponse.
- (b) Quelle fraction du nombre de biscuits mangés par Sarah correspond au nombre de biscuits mangés par Benoît? Justifie ta réponse.
- (c) Qui a mangé le moins de biscuits? Justifie ta réponse.
- (d) Quelqu'un a mangé 6 biscuits. Ce n'était pas la personne qui a mangé le plus ou le moins de biscuits. Combien de biscuits chaque personne a-t-elle mangés? Justifie ta réponse.





## Problem of the Week

### Problem A and Solution

### Cookies!

#### Problem

Benoit, Jin, Manuel, and Sarah shared a package of 30 cookies. After several days, all the cookies in the package were eaten by these four people and each person only ate whole cookies. Benoit recorded the following observations:

- Sarah ate twice as many cookies as Jin.
  - Manuel ate two-thirds as many cookies as Sarah.
  - Benoit ate half as many cookies as Manuel.
- (a) Who ate the most cookies? Justify your answer.
- (b) What fraction of the number of cookies eaten by Sarah is the number of cookies eaten by Benoit? Justify your answer.
- (c) Who ate the fewest cookies? Justify your answer.
- (d) Someone ate 6 cookies. This was not the person who ate the most or fewest cookies. How many cookies did each person eat? Justify your answer.

#### Solution

- (a) Since Sarah ate more cookies than Jin, we know that Jin did not eat the most cookies. Since Manuel ate fewer cookies than Sarah, we know that Manuel did not eat the most cookies. Since Benoit ate fewer cookies than Manuel, we know that Benoit did not eat the most cookies. Therefore, Sarah ate the most cookies.
- (b) Since Benoit ate half as many cookies as Manuel, and Manuel ate two-thirds as many cookies as Sarah, we need to calculate one-half of two-thirds, which is one-third. So Benoit ate one-third as many cookies as Sarah.
- (c) Since Sarah ate twice as many cookies as Jin, we can say that Jin ate one-half as many cookies as Sarah. From part (b) we know Benoit ate one-third as many cookies as Sarah. We also know that Manuel ate two-thirds as many cookies as Sarah. Since one-third is less than one-half, which is less than two-thirds, it follows that Benoit ate the fewest cookies.



- (d) Since we know that Sarah ate the most cookies, and Benoit ate the fewest cookies, then either Jin or Manuel ate 6 cookies. Let's guess that Jin ate 6 cookies.

In this case, from the first observation then Sarah ate  $2 \times 6 = 12$  cookies. We know that  $\frac{1}{3}$  of 12 is 4, so  $\frac{2}{3}$  of 12 is 8. From the second observation Manuel ate 8 cookies. From the third observation, Benoit ate  $\frac{1}{2}$  of 8, which is 4 cookies.

Since  $4 + 6 + 8 + 12 = 30$ , then it is possible that Benoit ate 4 cookies, Jin ate 6 cookies, Manuel ate 8 cookies, and Sarah ate 12 cookies.

We should also check to see if it is possible that Manuel was the person who ate 6 cookies. In this case, Benoit would have eaten  $\frac{1}{2}$  of 6, which is 3 cookies. From part (b) we noticed that Benoit ate  $\frac{1}{3}$  as many cookies as Sarah. This means we can say that Sarah ate 3 times as many cookies as Benoit, so Sarah would have eaten  $3 \times 3 = 9$  cookies. However, since Jin ate half as many cookies as Sarah, and one-half of 9 is not a whole number, that means Sarah could not have eaten 9 cookies. So Manuel could not be the person who ate 6 cookies.

We see that it must be the case that Benoit ate 4 cookies, Jin ate 6 cookies, Manuel ate 8 cookies, and Sarah ate 12 cookies.



## Problème de la semaine

### Problème A

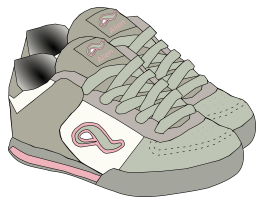
#### Horaire du gymnase

À l'école publique de Spruce Glen, chaque jour est divisé en neuf blocs. Chaque bloc a une durée de 30 minutes. Il y a six classes qui partagent le gymnase selon l'horaire hebdomadaire ci-dessous.

	Lundi	Mardi	Mercredi	Jeudi	Vendredi
<b>Bloc A</b>	Classe 1	Classe 3	Classe 2	Classe 3	Classe 6
<b>Bloc B</b>	Classe 5	Classe 5	Classe 2	Classe 3	Classe 1
<b>Bloc C</b>	Classe 3	Classe 5	Classe 2	Classe 2	Classe 3
<b>Bloc D</b>	Classe 3	Classe 5	Classe 5	Classe 2	Classe 3
<b>Bloc E</b>	Classe 6	Classe 1	Classe 5	Classe 6	Classe 3
<b>Bloc F</b>	Classe 4	Classe 2	Classe 6	Classe 1	Classe 5
<b>Bloc G</b>	Classe 4	Classe 6	Classe 1	Classe 1	Classe 2
<b>Bloc H</b>	Classe 2	Classe 4	Classe 3	Classe 4	Classe 2
<b>Bloc I</b>	Classe 2	Classe 4	Classe 4	Classe 5	Classe 4

- À l'aide d'un diagramme à bandes, représente le temps total par semaine que consacre chaque classe à faire du sport au gymnase.
- Classe, en ordre croissant, les classes selon le temps total par semaine qu'elles consacrent à faire du sport au gymnase.





## Problem of the Week

### Problem A and Solution

#### Gym Schedules

#### Problem

At Spruce Glen Public School, each day is divided into nine blocks, which are each 30 minutes long. There are six classrooms that share the gym, according to the weekly schedule shown.

	Monday	Tuesday	Wednesday	Thursday	Friday
<b>Block A</b>	Room 1	Room 3	Room 2	Room 3	Room 6
<b>Block B</b>	Room 5	Room 5	Room 2	Room 3	Room 1
<b>Block C</b>	Room 3	Room 5	Room 2	Room 2	Room 3
<b>Block D</b>	Room 3	Room 5	Room 5	Room 2	Room 3
<b>Block E</b>	Room 6	Room 1	Room 5	Room 6	Room 3
<b>Block F</b>	Room 4	Room 2	Room 6	Room 1	Room 5
<b>Block G</b>	Room 4	Room 6	Room 1	Room 1	Room 2
<b>Block H</b>	Room 2	Room 4	Room 3	Room 4	Room 2
<b>Block I</b>	Room 2	Room 4	Room 4	Room 5	Room 4

- (a) Make a bar chart showing the total gym time per week for each room.
- (b) List the rooms in order from least to greatest total gym time per week.

#### Solution

- (a) One way to draw the bar chart is to calculate the total gym time for each room. Then we can use the total times to determine the height of each bar. Remember that each block is 30 minutes long.

For example, if we add up the gym times for Room 1 in minutes we get:

- Monday time: 30 minutes
- Tuesday time: 30 minutes
- Wednesday time: 30 minutes
- Thursday time:  $30 + 30 = 60$  minutes
- Friday time: 30 minutes

Total time for Room 1 is  $30 + 30 + 30 + 60 + 30 = 180$  minutes





We could do these calculations for each room to get:

Total time for Room 2 is  $60 + 30 + 90 + 60 + 60 = 300$  minutes

Total time for Room 3 is  $60 + 30 + 30 + 60 + 90 = 270$  minutes

Total time for Room 4 is  $60 + 60 + 30 + 30 + 30 = 210$  minutes

Total time for Room 5 is  $30 + 90 + 60 + 30 + 30 = 240$  minutes

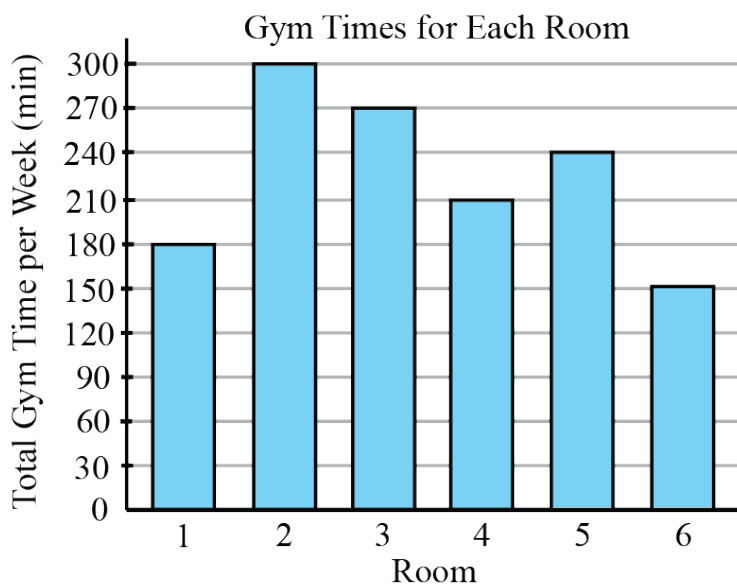
Total time for Room 6 is  $30 + 30 + 30 + 30 + 30 = 150$  minutes

Another way to build the bar chart is to count the total number of blocks that each class is in the gym. We can keep track of the number of blocks by using a tally chart.

Room	Number of Blocks
1	
2	
3	
4	
5	
6	

Then we can set our vertical axis to go up by 30 minute increments so that each tick mark in the bar chart represents one block in the gym.

The completed bar chart is shown.



(b) Looking at the size of the bars in the chart, the rooms in order from least to greatest total gym time per week is:

Room 6, Room 1, Room 4, Room 5, Room 3, Room 2



## Problème de la semaine

### Problème A

#### Être aux petits oiseaux

Le tableau suivant présente quelques informations sur certains des plus grands oiseaux du monde. Toutefois, le tableau est incomplet.

Oiseau	Taille moyenne (en cm)
Cygne muet	
Autruche	
Manchot royal	92
Condor des Andes	
Émeu	
Casoar à casque	155
Albatros hurleur	

- (a) Utilise les informations suivantes quant aux tailles moyennes des oiseaux pour remplir le restant du tableau:
- Le condor des Andes mesure 18 cm de plus que le manchot royal.
  - Le cygne muet mesure 55 cm de moins que le casoar à casque.
  - L'albatros hurleur mesure 7 cm de plus que le cygne muet.
  - L'autruche mesure 1 m de plus que le condor des Andes.
  - Le casoar à casque mesure 20 mm de plus que l'émeu.
- (b) Classe les oiseaux selon leur taille du plus petit au plus grand.



## Problem of the Week

### Problem A and Solution

### Going to the Birds

#### Problem

The following table shows some information about some of the world's tallest birds. However, the table is incomplete.

Bird	Average Height (in cm)
Mute Swan	
Ostrich	
King Penguin	92
Andean Condor	
Emu	
Southern Cassowary	155
Wandering Albatross	

- (a) Use the following information about the average heights of these birds to fill in the rest of the table:
- The Andean Condor is 18 cm taller than the King Penguin.
  - The Mute Swan is 55 cm shorter than the Southern Cassowary.
  - The Wandering Albatross is 7 cm taller than the Mute Swan.
  - The Ostrich is 1 m taller than the Andean Condor.
  - The Southern Cassowary is 20 mm taller than the Emu.
- (b) List the birds in order from shortest to tallest.

**Solution**

- (a) Since the Andean Condor is 18 cm taller than the King Penguin, the Andean Condor is  $92 + 18 = 110$  cm tall.

Since the Mute Swan is 55 cm shorter than the Southern Cassowary, the Mute Swan is  $155 - 55 = 100$  cm tall.

Since the Wandering Albatross is 7 cm taller than the Mute Swan, the Wandering Albatross is  $100 + 7 = 107$  cm tall.

Since the Ostrich is 1 m taller than the Andean Condor, and  $1 \text{ m} = 100 \text{ cm}$ , the Ostrich is  $110 + 100 = 210$  cm tall.

Since the Southern Cassowary is 20 mm taller than the Emu, and  $20 \text{ mm} = 2 \text{ cm}$ , the Emu is  $155 - 2 = 153$  cm tall.

The completed version of the table is:

<b>Bird</b>	<b>Average Height (in cm)</b>
Mute Swan	100
Ostrich	210
King Penguin	92
Andean Condor	110
Emu	153
Southern Cassowary	155
Wandering Albatross	107

- (b) We can rank the birds from shortest to tallest using the completed table from part (a). From shortest to tallest, the birds are:  
King Penguin, Mute Swan, Wandering Albatross, Andean Condor, Emu, Southern Cassowary, Ostrich



## Problème de la semaine

### Problème A

#### L'addition et la soustraction

Suis les étapes ci-dessous.

**Étape 1:** Choisis deux nombres différents de trois chiffres. Soit  $A$  le plus grand des deux nombres et  $B$  le plus petit.

**Étape 2:** Soustrais  $B$  de 999; soit  $C$  la différence obtenue.

**Étape 3:** Additionne  $A$  et  $C$ ; soit  $D$  la somme obtenue.

**Étape 4:** Soustrais 1000 de  $D$ ; soit  $E$  la différence obtenue.

**Étape 5:** Ajoute 1 à  $E$ ; soit  $F$  la somme obtenue.

- (a) Quel est le lien entre le nombre  $F$  et les nombres  $A$  et  $B$ ?
- (b) Essaie les mêmes étapes avec des nombres différents. Penses-tu que tu obtiendras toujours le même résultat? Explique pourquoi.





## Problem of the Week

### Problem A and Solution

### Adding and Subtracting

#### Problem

Follow the steps below.

**Step 1:** Pick two different three-digit numbers. Label the larger number  $A$  and the smaller number  $B$ .

**Step 2:** Subtract  $B$  from 999 and label the difference  $C$ .

**Step 3:** Add  $A$  and  $C$  and label the sum  $D$ .

**Step 4:** Subtract 1000 from  $D$  and label the difference  $E$ .

**Step 5:** Add 1 to  $E$  and label the sum  $F$ .

- (a) What is the connection between the number  $F$  and the numbers  $A$  and  $B$ ?
- (b) Try the same steps with different numbers. Do you think you will always get the same result? Why or why not?

#### Solution

- (a) We can work through this procedure with any two, random, three-digit numbers. Let's try starting with 814 and 275.

**Step 1:** The larger number 814 is labelled  $A$ , and the smaller number 275 is labelled  $B$ .

**Step 2:** The difference  $999 - B$  is  $999 - 275 = 724$ , and is labelled  $C$ .

**Step 3:** The sum  $A + C$  is  $814 + 724 = 1538$ , and is labelled  $D$ .

**Step 4:** The difference  $D - 1000$  is  $1538 - 1000 = 538$ , and is labelled  $E$ .

**Step 5:** The sum  $E + 1$  is  $538 + 1 = 539$ , and is labelled  $F$ .

Notice that  $814 - 275 = 539$ . So  $A - B = F$ .

- (b) If you try this procedure with any two three-digit numbers, it will always work out that  $A - B = F$ . We will show this using algebra.

**Step 1:** We choose three-digit numbers  $A$  and  $B$  so that  $A \geq B$ .

**Step 2:** We calculate  $999 - B$ , and label this  $C$ . That is,  $C = 999 - B$ .

**Step 3:** We add  $A + C$ . So, we calculate  $A + 999 - B$ , and label this  $D$ . That is,  $D = A + 999 - B$ .

**Step 4:** We subtract 1000 from  $D$ . So, we calculate  $A + 999 - B - 1000$ , and label this  $E$ . That is,  $E = A + 999 - B - 1000$ .

**Step 5:** We add 1 to  $E$ . So, we calculate  $A + 999 - B - 1000 + 1$ , and label this  $F$ . That is,  $F = A + 999 - B - 1000 + 1$ .

Now, we can simplify this expression to get  $A - B + 999 - 1000 + 1 = A - B$ , since  $999 - 1000 + 1 = 0$ . So,  $F = A - B$ .









## Solution

- (a) We can make a table showing the number of stitches in each row as we follow the pattern.

Rows	Number of Stitches
1 – 6	35
7 – 12	37
13 – 18	39
19 – 24	41

Since 20 is between 19 and 24, there will be 41 stitches in the 20<sup>th</sup> row.

- (b) We can make a table showing the row number and the length of the item after that row has been knitted. Here we will use skip counting and look at the length after every 6<sup>th</sup> row.

Row	Length (in cm)
6	3
12	6
18	9
24	12
30	15
36	18
42	21
48	24
54	27
60	30

After 60 rows, our finished item will have a length of 30 cm.

- (c) We can make another table showing the number of stitches in each row, again using skip counting and looking at every 6<sup>th</sup> row up to row 60.

Row	Number of Stitches
6	35
12	37
18	39
24	41
30	43
36	45
42	47
48	49
54	51
60	53

The 60<sup>th</sup> row will have 53 stitches.



## Problème de la semaine

### Problème A

#### Jouer à la balle

Laure adore jouer à la balle avec son chien Spencer. Avant que Laure ne lance la balle, Spencer est positionné à côté d'elle. Lorsque Laure lance la balle, Spencer court vers la balle et la ramène à Laure. Laure lance la balle trois fois.

- La première fois, Laure lance la balle à une distance de 8 mètres.
- La deuxième fois, elle lance la balle deux fois plus loin que la première fois.
- La troisième fois, elle lance la balle 5 mètres moins loin que la deuxième fois.

Quelle distance Spencer a-t-il parcourue en tout?





## Problem of the Week

### Problem A and Solution

#### Playing Fetch

#### Problem

Leslie loves playing fetch with her dog Spencer. Spencer always starts by sitting beside Leslie before Leslie throws the ball. When Leslie throws the ball, Spencer runs to it and brings the ball back to the same spot. Leslie throws the ball three times.

- The first time she throws it 8 metres.
- The second time she throws it twice as far as the first time.
- The third time she throws it 5 metres less than the second time.

How far does Spencer run in total?

#### Solution

On the first throw, Spencer runs  $2 \times 8 = 16$  metres.

The distance of the second throw is  $8 \times 2 = 16$  metres.

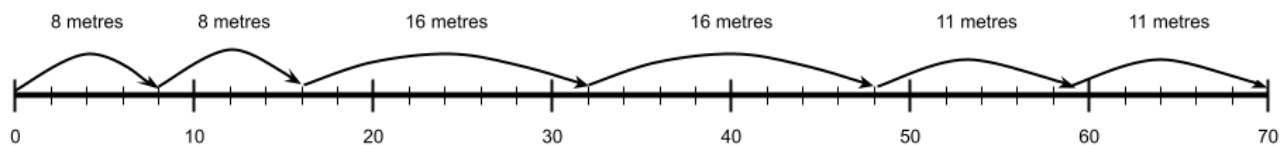
On the second throw, Spencer runs  $2 \times 16 = 32$  metres.

The distance of the third throw is  $16 - 5 = 11$  metres.

On the third throw, Spencer runs  $2 \times 11 = 22$  metres.

The total distance Spencer runs is:  $16 + 32 + 22 = 70$  metres.

We can also show the distance Spencer runs on a number line.





## Problème de la semaine

### Problème A

#### Diagramme de Carroll

Les diagrammes de Carroll sont des tableaux que l'on peut utiliser pour classer des objets en fonction de deux propriétés. Le tableau comporte deux rangées et deux colonnes. Les rangées servent à trier en fonction de la présence ou non de la première propriété et les colonnes servent à trier en fonction de la présence ou non de la deuxième propriété. À l'intersection d'une rangée et d'une colonne se trouve une cellule qui contient des objets possédant les deux propriétés identifiées par le titre de la rangée et celui de la colonne.

Classe les nombres suivants dans le diagramme de Carroll ci-dessous:

12, 63, 15, 150, 56, 30, 55, 21, 88, 72

Le premier nombre a déjà été placé dans le tableau. Le nombre 12 a été placé dans la cellule qui doit contenir des nombres pairs qui sont également des multiples de 3.

	Nombre pair	Nombre impair
Multiple de 3	12	
N'est pas un multiple de 3		

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## Problem of the Week

### Problem A and Solution

### Carroll Diagram

#### Problem

Carroll diagrams are tables that you use to sort objects based on two properties. The table has two rows and two columns. The rows are for sorting based on whether or not the one property is present and the columns are for sorting based on whether or not the second property is present. At the intersection of a row and column is a cell that contains objects that have both properties identified by the row and column labels.

Arrange the following numbers into the Carroll diagram below:

12, 63, 15, 150, 56, 30, 55, 21, 88, 72

	Even Number	Odd Number
Multiple of 3	12	
Not a Multiple of 3		

The first number has been placed in the diagram already. The number 12 has been added to the cell that is at the intersection of the 'Even Number' column and the 'Multiple of 3' row.

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#### Solution

Here is the completed Carroll diagram:

	Even Number	Odd Number
Multiple of 3	12, 150, 30, 72	63, 15, 21
Not a Multiple of 3	56, 88	55

A quick trick to determine if a number is a multiple of 3 is to calculate the sum of its digits. If the sum of the digits is a multiple of 3, then the original number is also a multiple of 3. For example, for the number 72, the sum of the digits is  $7 + 2 = 9$ . Since the sum of 9 is divisible by 3, then 72 is also divisible by 3. Also, for the number 88, the sum of the digits is  $8 + 8 = 16$ . Since 16 is not divisible by 3, then 88 is not divisible by 3.



## Problème de la semaine

### Problème A

#### Décisions de données

La famille Webb essaie de se décider pour l'achat d'un nouveau plan mensuel de données Internet. Trois choix s'offrent à elle:

Plan A: 10 \$ pour les 10 premiers Go de données et 5 \$ pour chaque 2 Go supplémentaires.

Plan B: 40 \$ pour les 20 premiers Go de données et 10 \$ pour chaque 10 Go supplémentaires.

Plan C: 80 \$ pour un nombre illimité de Go de données.

Remarque que pour le plan A, les données supplémentaires doivent être achetées par tranches de 2 Go. De même, pour le plan B, les données supplémentaires doivent être achetées par tranches de 10 Go.

Sachant que la famille utilisera entre 25 et 40 Go de données chaque mois, quel plan la famille Webb devrait-elle choisir ? Justifie ta réponse.





## Problem of the Week

### Problem A and Solution

#### Deciding About Data

#### Problem

The Webb family is trying to decide on a new monthly internet plan. There are three choices:

Plan A: \$10 for the first 10 GB of data, and each additional 2 GB costs \$5.

Plan B: \$40 for the first 20 GB of data, and each additional 10 GB costs \$10.

Plan C: \$80 for unlimited GB of data.

Note that for Plan A, additional data has to be purchased in 2 GB increments. Similarly, for Plan B, additional data has to be purchased in 10 GB increments.

After keeping track of data used, the family decides they will use between 25 GB and 40 GB of data each month. Which plan should the Webb family choose? Justify your answer.

#### Solution

One way to make a decision is to make a table showing how much each plan would cost for various amounts of data use.

Data Used (in GB)	Total Cost (in \$) for Plan A	Total Cost (in \$) for Plan B	Total Cost (in \$) for Plan C
10	10	40	80
12	15	40	80
14	20	40	80
16	25	40	80
18	30	40	80
20	35	40	80
22	40	50	80
24	45	50	80
26	50	50	80
28	55	50	80
30	60	50	80
32	65	60	80
34	70	60	80
36	75	60	80
38	80	60	80
40	85	60	80

Notice that at 25 GB, with Plan A they would need to get 26 GB of data. This would cost \$50. So, comparing the cost of the plans, we notice that Plan B is the lowest price from 25 GB to 40 GB. Therefore, the family should choose Plan B.

(Note that if the family uses less than 25 GB per month, then Plan A is better. Also, if they use more than 40 GB, then it looks like Plan B is better at first, but Plan C will eventually be better.)

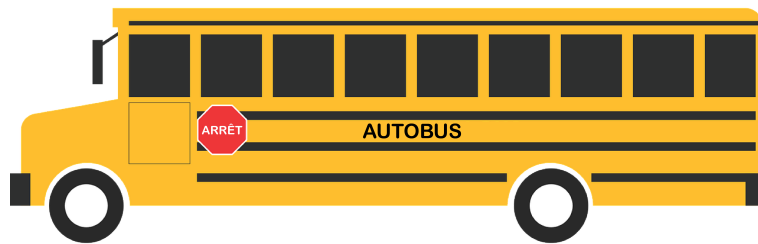


## Problème de la semaine

### Problème A

#### Sortie au théâtre

Les classes de 3<sup>e</sup> et 4<sup>e</sup> années vont faire une sortie scolaire au théâtre. Il y a 143 élèves, 6 membres du personnel enseignant et 16 parents bénévoles qui se rendront au théâtre en autobus scolaire. Si chaque autobus peut transporter au maximum 45 passagers, quel est le plus petit nombre d'autobus nécessaires pour cette sortie ?







## Problem of the Week

### Problem A and Solution

### Theatre Trip

#### Problem

The Grade 3 and Grade 4 classes are going on a field trip to the theatre. There are 143 students, 6 teachers, and 16 parent volunteers that will be travelling by school bus to the theatre. If each bus is limited to 45 passengers, what is the fewest number of buses needed for the trip?

#### Solution

First we need to calculate how many people will be travelling in total.

There is a total of  $143 + 6 + 16 = 165$  people on the field trip.

Now we can make a table that shows how many people can be transported on buses that hold 45 people each:

Number of Buses	Number of People
1	45
2	90
3	135
4	180

From this table, we see that 3 buses will not hold enough people for the trip, but 4 buses will have enough room for everybody. Therefore, the fewest number of buses needed is 4.

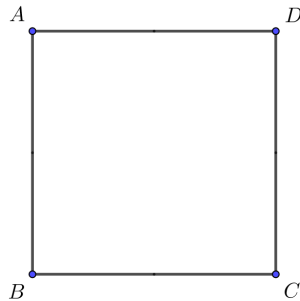


## Problème de la semaine

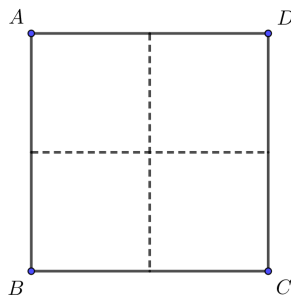
### Problème A

### Origami

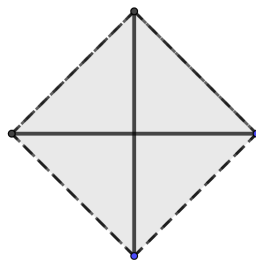
Laila commence avec une feuille de papier carrée. En commençant par un coin et en se déplaçant autour du carré, elle nomme les coins  $A$ ,  $B$ ,  $C$  et  $D$ .



Laila plie le papier en deux, en repliant le côté  $AB$  sur le côté  $DC$  de manière à former un rectangle. Elle déplie le papier et le plie à nouveau, cette fois-ci en pliant le côté  $AD$  sur le côté  $BC$ , de manière à former un autre rectangle. Lorsqu'elle déplie le papier à nouveau, elle voit deux plis dans le papier, comme dans la figure ci-dessous.



Le centre du carré est le point où les deux plis se coupent. Ensuite, elle prend chaque coin du carré et plie le papier de manière que chacun des coins touche le centre du carré. En pliant les quatre coins de cette manière, elle obtient un autre carré plus petit composé de quatre régions triangulaires, comme dans la figure ci-dessous.



Quelle fraction de l'aire du grand carré original représente l'aire du petit carré? Justifie ta réponse.



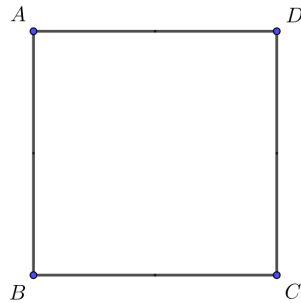
# Problem of the Week

## Problem A and Solution

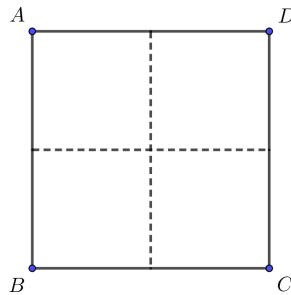
### Origami

#### Problem

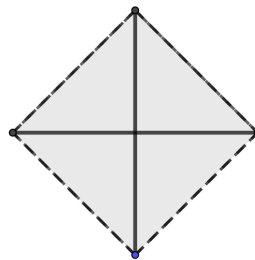
Laila starts with a square piece of paper. Starting at one corner and moving around the square, she labels the corners  $A$ ,  $B$ ,  $C$ , and  $D$ .



Laila folds the paper in half, by folding side  $AB$  onto side  $DC$ , to form a rectangle. She opens up the paper and folds it again to form another rectangle by folding side  $AD$  onto side  $BC$ . When she opens up the paper this time, she sees two creases in the paper as shown below.



The centre of the square is the point where the two creases intersect. Now, she takes each corner of the square and folds the paper so that each corner touches the centre of the square. Folding all four corners in this way forms another smaller square made up of four triangular regions as shown below.



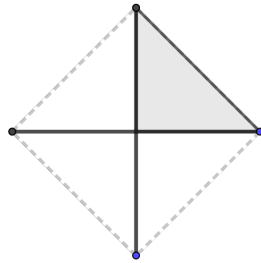
What fraction of the area of the original square is the area of this smaller square? Justify your answer.



### Solution

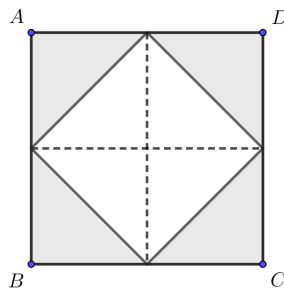
The smaller square has an area that is  $\frac{1}{2}$  the area of the original square. A justification of this is given below.

Consider the following image of the smaller square with only one of the four triangular regions shaded.



Underneath the shaded triangle is a region of the original square that is exactly the same size. That is true for all four of the triangles that were formed by having the corners meet at the centre of the original square.

Let's now shade all four of the triangular regions in the smaller square, and then open up the paper again.



We can make the following observations:

- The shaded triangles each have a matching unshaded triangle.
- The shaded triangles make up the area of the smaller square.
- The area of the original square is equal to the area of the shaded triangles plus the area of the smaller square. This means the area of the original square is 2 times the area of the smaller square.

It follows that the area of the smaller square is  $\frac{1}{2}$  the area of the original square.




## Problème de la semaine


### Problème A

#### Les comptes à la confiserie

Ricardo et Nadia sont allés à la confiserie. Les indices ci-dessous décrivent les sortes et les quantités de bonbons qu'ils ont achetés.

- Ils ont acheté 8 paquets de Sunbursts.
- Ils ont acheté 4 paquets de Twinglers de plus que de paquets de Sunbursts.
- Ils ont acheté 6 paquets de Nerts de moins que de paquets de Twinglers.
- Ils ont acheté deux fois plus de paquets de W&Ws que de paquets de Nerts.
- Le nombre de paquets de Sweet Patch Kids est égal au nombre total de paquets de Sunbursts et de Nerts.
- Le nombre de paquets de Jolly Farmers est égal au nombre de paquets de Sweet Patch Kids moins le nombre de paquets de Twinglers.

Complète le pictogramme afin de représenter le nombre de paquets de chaque sorte de bonbons qu'ils ont acheté. Utilise un  pour représenter deux paquets de bonbons. À titre d'exemple, la première ligne a déjà été remplie.

Sorte de bonbons	Nombre de paquets
Sunbursts	
Twinglers	
Nerts	
W&Ws	
Sweet Patch Kids	
Jolly Farmers	

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# Problem of the Week

## Problem A and Solution


### Candy Store Counting


#### Problem

Ricardo and Nadia went to the candy store. The clues below describe the types and amount of candies they bought.

- They bought 8 packages of Sunbursts.
- They bought 4 more packages of Twinglers than Sunbursts.
- They bought 6 fewer packages of Nerts than Twinglers.
- They bought twice as many packages of W&Ws than Nerts.
- The number of packages of Sweet Patch Kids is equal to the total number of packages of Sunbursts and Nerts.
- The number of packages of Jolly Farmers is equal to the number of packages of Sweet Patch Kids minus the number of packages of Twinglers.

Complete the pictograph to show how many packages of each type of candy they purchased.

Use one  to represent two packages of candy. The first row has already been completed for you.

Type of Candy	Number of Packages
Sunbursts	
Twinglers	
Nerts	
W&Ws	
Sweet Patch Kids	
Jolly Farmers	



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## Solution

First we need to calculate how many packages of each kind of candy they bought. We know they bought 8 packages of Sunbursts.

- Buying 4 more packages of Twinglers than Sunbursts means they bought  $8 + 4 = 12$  packages of Twinglers.
- Buying 6 fewer packages of Nerts than Twinglers means they bought  $12 - 6 = 6$  packages of Nerts.
- Buying twice as many packages of W&Ws than Nerts means they bought  $6 \times 2 = 12$  packages of W&Ws.
- The number of packages of Sweet Patch Kids they bought is  $8 + 6 = 14$ .
- The number of packages of Jolly Farmers they bought is  $14 - 12 = 2$ .

To complete the pictograph, we use  to represent two packages of candy. So we divide the number of packages for each type of candy by 2, in order to calculate the number of  needed for that candy in the pictograph.

The completed pictograph is shown below.

Type of Candy	Number of Packages
Sunbursts	   
Twinglers	     
Nerts	  
W&Ws	     
Sweet Patch Kids	      
Jolly Farmers	

**Key:** one  represents 2 packages of candy.



## Problème de la semaine

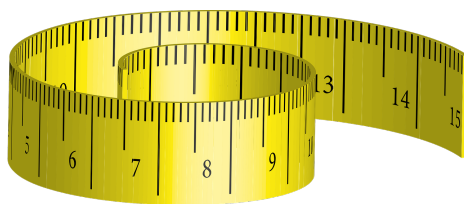
### Problème A

#### Mesurez-moi

Arezoo, Femke, Jackson, Nya et Élisabeth ont créé un tableau dans lequel ils ont inscrit leurs tailles à différents âges de leur vie.

Nom	Taille à la naissance	Taille à l'âge de 6 ans	Taille adulte
Arezoo	44 cm	106 cm	1,51 m
Femke	47 cm	104 cm	153 cm
Jackson	49 cm	108 cm	2 m
Nya	48 cm	1,11 m	189 cm
Élisabeth	52 cm	1 m et 19 cm	1,84 m

- (a) Qui a le plus grandi entre la naissance et l'âge de 6 ans ? Qui a le moins grandi entre la naissance et l'âge de 6 ans ? Justifie tes réponses.
- (b) À l'aide de l'estimation, écris la liste d'amis en ordre croissant de croissances (soit de la croissance la moins élevée à la croissance la plus élevée) entre l'âge de 6 ans et l'âge adulte.







## Problem of the Week

### Problem A and Solution

### Measure Me

#### Problem

Arezoo, Femke, Jackson, Nya, and Elisabeth made a table that recorded their heights at different stages of their lives.

Name	Height at Birth	Height at Age 6	Adult Height
Arezoo	44 cm	106 cm	1.51 m
Femke	47 cm	104 cm	153 cm
Jackson	49 cm	108 cm	2 m
Nya	48 cm	1.11 m	189 cm
Elisabeth	52 cm	1 m and 19 cm	1.84 m

- (a) Who grew the most between birth and age 6? Who grew the least between birth and age 6? Justify your answers.
- (b) Using estimation, arrange the list of friends from least growth to most growth from age 6 to adulthood.

#### Solution

- (a) One way to solve this is to convert all of the measurements into centimetres and then find the difference between each person's height at age 6 and at birth.

Name	Height at Birth	Height at Age 6	Height Difference
Arezoo	44 cm	106 cm	$106 - 44 = 62$ cm
Femke	47 cm	104 cm	$104 - 47 = 57$ cm
Jackson	49 cm	108 cm	$108 - 49 = 59$ cm
Nya	48 cm	111 cm	$111 - 48 = 63$ cm
Elisabeth	52 cm	119 cm	$119 - 52 = 67$ cm

Elisabeth grew the most between birth and age 6.  
Femke grew the least between birth and age 6.



- (b) We will estimate the growth of each person by rounding numbers to the nearest 10 cm.

Name	Approximate Height at Age 6	Approximate Adult Height	Approximate Difference
Arezoo	110 cm	150 cm	$150 - 110 = 40$ cm
Femke	100 cm	150 cm	$150 - 100 = 50$ cm
Jackson	110 cm	200 cm	$200 - 110 = 90$ cm
Nya	110 cm	190 cm	$190 - 110 = 80$ cm
Elisabeth	120 cm	180 cm	$180 - 120 = 60$ cm

When we list the friends in order by approximate growth between age 6 and adulthood, from least growth to most growth, we get:

Arezoo, Femke, Elisabeth, Nya, and Jackson

It turns out that if we determine the actual difference between each person's adult height and height at age 6, and then list the friends in order from least growth to most growth, we would get the same ordering. However, this will not always be the case. For example, if Arezoo's adult height had been 1.54 m and Femke's adult height had been 151 cm, then the order when approximating would have been the same as above, but the actual order would have been Femke, Arezoo, Elisabeth, Nya, Jackson.



## Problème de la semaine

### Problème A

#### Problèmes d'aquarium

Jacques a reçu un aquarium pour son anniversaire et veut le remplir avec des guppys et des tétras. Les guppys sont vendus par groupes de quatre et les tétras par groupes de trois. Il peut acheter quatre guppys pour 12 \$ et trois tétras pour 7 \$.

Si Jacques a dépensé exactement 50 \$ pour acheter des poissons, combien de poissons de chaque type a-t-il acheté?





## Problem of the Week

### Problem A and Solution

#### Aquarium Issues

#### Problem

Jacques got an aquarium for his birthday and wants to fill it with some guppies and tetras. Guppies are sold in groups of four and tetras are sold in groups of three. He can buy four guppies for \$12, and three tetras for \$7.

If Jacques spent exactly \$50 on fish, how many of each fish did he buy?

#### Solution

Since 50 is not a multiple of 12 or a multiple of 7, then Jacques must have bought some of each fish in order to spend exactly \$50. One way to solve this problem is to make a table to keep track of how much money it costs for multiples of four guppies, and how much of the \$50 would be left to buy tetras.

Number of Guppies	Cost for Guppies (in \$)	Money Leftover for Tetras (in \$)
4	$1 \times 12 = 12$	$50 - 12 = 48$
8	$2 \times 12 = 24$	$50 - 24 = 26$
12	$3 \times 12 = 36$	$50 - 36 = 14$
16	$4 \times 12 = 48$	$50 - 48 = 2$

Now we look for a multiple of seven in the leftover money, because each group of tetras costs \$7. The only multiple of seven in the leftover money is 14. Since  $14 = 2 \times 7$ , Jacques must have bought two groups of tetras.

This means Jacques bought 12 guppies and  $2 \times 3 = 6$  tetras.



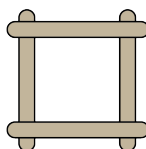
## Problème de la semaine

### Problème A

#### Construction artisanale

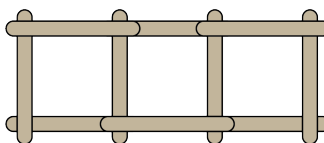
Sam fabrique des cadres photo carrés avec des bâtonnets de bois. Il a une boîte de 50 bâtonnets de bois et veut fabriquer 13 cadres.

- (a) Sam prévoit fabriquer des cadres individuels en utilisant quatre bâtonnets de bois comme dans la figure ci-dessous.



Aura-t-il assez de bâtonnets pour fabriquer 13 cadres? Justifie ta réponse.

- (b) Sam change d'avis et, au lieu de fabriquer des cadres individuels, il décide de relier les cadres en une rangée. Il commence par fabriquer un cadre à l'aide de quatre bâtonnets de bois, puis crée un deuxième cadre attaché au premier en utilisant trois bâtonnets. Il rajoute ensuite trois autres bâtonnets pour créer un troisième cadre attaché aux deux premiers, comme dans la figure ci-dessous.



Sam prévoit poursuivre ce processus, en utilisant trois bâtonnets de bois supplémentaires pour chaque cadre, jusqu'à ce qu'il ait en tout 13 cadres qui soient reliés en rangée. Aura-t-il assez de bâtonnets de bois pour fabriquer 13 cadres? Justifie ta réponse.

- (c) Peux-tu dessiner une autre disposition des 13 cadres que Sam aurait pu construire en utilisant au maximum 50 bâtonnets de bois? Combien de bâtonnets de bois as-tu utilisé dans ton dessin?
- (d) Peux-tu dessiner une disposition des 13 cadres qui contient moins de 35 bâtonnets de bois?



# Problem of the Week

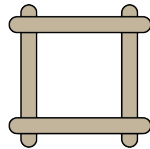
## Problem A and Solution

### Crafty Construction

#### Problem

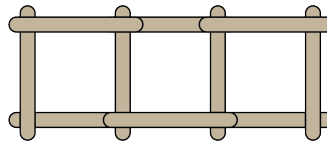
Sam is making square picture frames using popsicle sticks. He has one box of 50 popsicle sticks and wants to make 13 frames.

- (a) Sam plans to make individual frames using four popsicle sticks as shown.



Will he have enough popsicle sticks to make 13 frames? Justify your answer.

- (b) Sam changes his mind and instead of individual frames, he decides to connect the frames in a row. He starts by making a frame using four popsicle sticks, and then uses three popsicle sticks to create another frame attached to this frame. He then uses three more popsicle sticks to create another frame attached to the first two frames, so he has three connected frames, as shown.



Sam plans to continue this process, using three more popsicle sticks for each frame, until he has 13 frames connected in a row. Will he have enough popsicle sticks to make 13 frames? Justify your answer.

- (c) Can you draw another layout of the 13 frames that Sam could have built using at most 50 popsicle sticks? How many popsicle sticks does your layout use?
- (d) Can you draw a layout of the 13 frames that uses fewer than 35 popsicle sticks?



## Solution

- (a) Since each frame requires 4 popsicle sticks, the total number of popsicle sticks required for 13 frames is equal to  $13 \times 4 = 52$ .

Alternatively, we could make a table showing the number of frames and the number of popsicle sticks required.

Number of Frames	Number of Popsicle Sticks
1	4
2	8
3	12
4	16
5	20
6	24
7	28
8	32
9	36
10	40
11	44
12	48
13	52

Either way, since it will take 52 popsicle sticks to make 13 individual frames, Sam will not have enough popsicle sticks to make all the frames.

- (b) The first frame uses 4 popsicle sticks but the other 12 frames use only 3 popsicle sticks each. So the total number of popsicle sticks required can be found by adding 4 to  $12 \times 3$ . Since  $12 \times 3 = 36$ , this gives a total of  $4 + 36 = 40$  popsicle sticks.

Alternatively, we could make a table showing the number of frames and the number of popsicle sticks required.

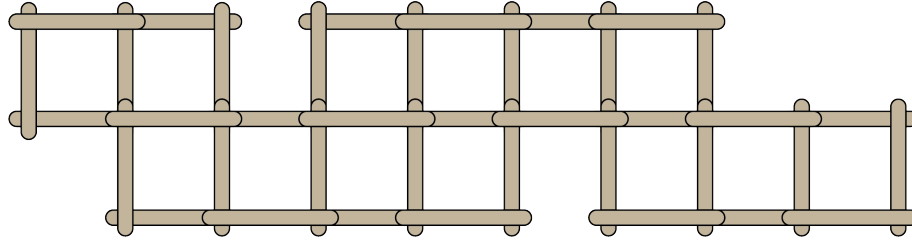
Number of Frames	Number of Popsicle Sticks
1	4
2	7
3	10
4	13
5	16
6	19
7	22
8	25
9	28
10	31
11	34
12	37
13	40

Either way, since it will take 40 popsicle sticks to build a row of 13 connected frames, Sam will have enough popsicle sticks to make all the frames.

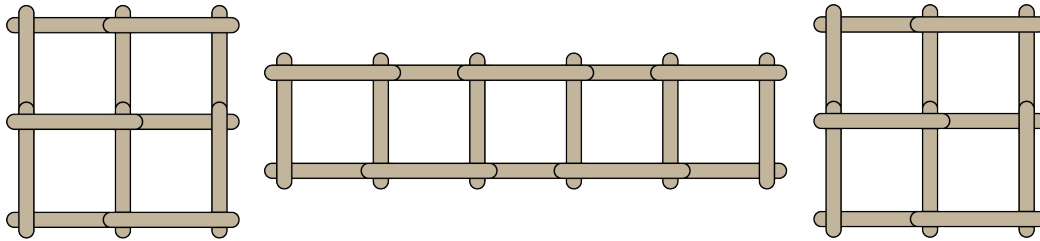


- (c) There are many layouts of 13 frames you could make using at most 50 popsicle sticks. Two examples are shown.

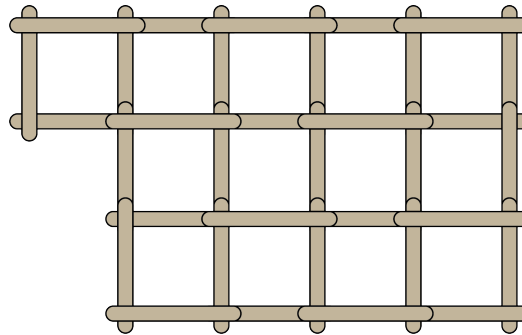
The following layout uses 39 popsicle sticks.



The following layout uses 40 popsicle sticks.



- (d) The most efficient use of popsicle sticks is to share as many sides as possible with other frames. If you connect the frames to form a shape as close as possible to a square, you can make 13 frames using only 34 popsicle sticks, as shown.





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# Géométrie et mesure (G)

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## Problème de la semaine

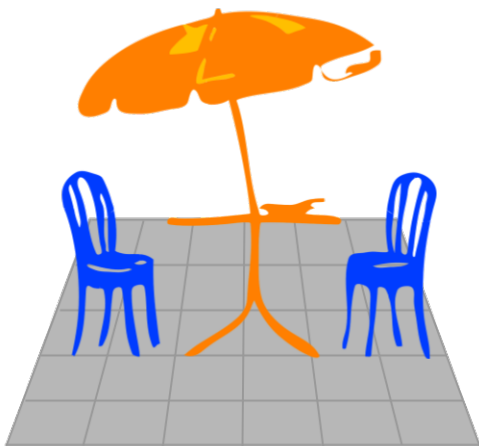
### Problème A

#### Conception de terrasse

Jody et Jillian veulent construire une terrasse derrière leur maison. Ils comptent utiliser des pierres carrées dont les côtés ont une longueur de 50 cm. Ils ont, en tout, 75 pierres carrées disponibles.

Pour construire la terrasse, ils placent les pierres carrées de manière à ce que deux pierres côte à côte se touchent et que leurs côtés soient parfaitement alignés. Ils n'utiliseront que des pierres carrées entières et ils veulent que toute la terrasse soit entièrement recouverte de pierres.

- (a) S'ils voulaient que leur terrasse ait la forme d'un carré, quelles sont les dimensions de la plus grande terrasse qu'ils pourraient construire?
- (b) S'ils voulaient que leur terrasse ait la forme d'un rectangle dont la longueur d'un côté est le double de la longueur de l'autre côté, quelles sont les dimensions de la plus grande terrasse qu'ils pourraient construire?





## Problem of the Week

### Problem A and Solution

### Patio Planning

#### Problem

Jody and Jillian are building a patio beside their house. They have square patio stones that have sides with a length of 50 cm. They have a total 75 patio stones available.

To build the patio, they place the patio stones so that two stones next to each other are touching and their sides are lined up exactly. They will only use whole patio stones and they want the entire patio covered in stones.

- (a) If they want to have their patio in the shape of a square, what are the dimensions of the largest possible patio they can build?
- (b) If they want to build a patio in the shape of a rectangle where the length of one side is twice as long as the length of the other side, what are the dimensions of the largest patio they can build?

#### Solution

- (a) The following table shows the possible sizes of the patio if the patio is in the shape of a square.

Length	Width	Number of Stones Used
1	1	$1 \times 1 = 1$
2	2	$2 \times 2 = 4$
3	3	$3 \times 3 = 9$
4	4	$4 \times 4 = 16$
5	5	$5 \times 5 = 25$
6	6	$6 \times 6 = 36$
7	7	$7 \times 7 = 49$
8	8	$8 \times 8 = 64$
9	9	$9 \times 9 = 81$

Since there are only 75 patio stones available, the biggest square patio that Jody and Jillian can build is 8 patio stones long by 8 patio stones wide. Since each square patio stone has sides with length 50 cm, then 8 stones in a line have a length of  $8 \times 50 = 400$  cm or 4 metres. So the largest square patio made out of 75 or fewer patio stones has dimensions 4 meters long by 4 metres wide.



- (b) To investigate a patio that has one side that is twice as long as the other side, we can name the shorter side Length and the longer side Width. The following table shows the possible sizes of the patio.

Length	Width	Number of Stones Used
1	2	$1 \times 2 = 2$
2	4	$2 \times 4 = 8$
3	6	$3 \times 6 = 18$
4	8	$4 \times 8 = 32$
5	10	$5 \times 10 = 50$
6	12	$6 \times 12 = 72$
7	14	$7 \times 14 = 98$

Since we only have 75 patio stones, the biggest patio Jody and Jillian can build that has one side twice as long as the other side is a rectangle that is 6 patio stones long by 12 patio stones wide. Since each square patio stone has sides with length 50 cm, then 6 stones in a line have a length of  $6 \times 50 = 300$  cm or 3 metres, and 12 stones in a line have a length of  $12 \times 50 = 600$  cm or 6 metres. So the largest patio with one side twice as long as the other side and made out of 75 or fewer patio stones, has dimensions 3 metres by 6 metres.



## Problème de la semaine

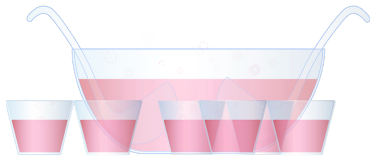
### Problème A

#### Un punch parfait

Su prépare du punch pour ses camarades. Elle veut mélanger 3 L de jus d'orange, 1 L de boisson gazeuse,  $\frac{1}{2}$  L de jus de raisin et 300 mL de jus de canneberge dans un bol à punch.

- (a) Pour prévenir les dégâts, Su prévoit d'utiliser un bol à punch dont la capacité doit dépasser d'au moins 200 mL le volume du liquide qu'il contiendra. Quelle est la plus petite capacité que devrait avoir son bol à punch?
- (b) Su a des verres qui peuvent contenir chacun 300 mL de punch. Combien de ces verres peut-elle remplir avec le punch qu'elle prépare?





## Problem of the Week

### Problem A and Solution

#### Perfect Punch

#### Problem

Su is going to make punch for her friends. She wants to mix 3 L of orange juice, 1 L of pop,  $\frac{1}{2}$  L of grape juice, and 300 mL of cranberry juice in a punch bowl.

- To avoid spilling, Su plans to use a punch bowl with a capacity of at least 200 mL more than the liquid it holds. What is the smallest capacity that her punch bowl should have?
- Su has cups that can each hold 300 mL of punch. How many of these cups can she fill with the punch she makes?

#### Solution

- The smallest capacity of the punch bowl is the sum of the volumes of each liquid, plus the 200 mL of extra space to avoid spilling.

One way to calculate this would be to convert all the volumes to millilitres.

- 3 L = 3000 mL
- 1 L = 1000 mL
- $\frac{1}{2}$  L = 500 mL

So the minimum capacity is  $3000 + 1000 + 500 + 300 + 200 = 5000$  mL.

Alternatively, we might notice that the sum of the volume of cranberry juice and the extra room for spillage is:  $300 + 200 = 500$  mL or  $\frac{1}{2}$  L.

So the minimum capacity is  $3 + 1 + \frac{1}{2} + \frac{1}{2} = 5$  L.

- The volume of punch is  $3000 + 1000 + 500 + 300 = 4800$  mL.

We can use skip counting to figure out how many cups of punch Su can fill:

300, 600, 900, 1200, 1500, 1800, 2100, 2400, 2700, 3000, 3300, 3600, 3900, 4200, 4500, 4800

We can see from this that Su can fill 16 cups with punch.

Alternatively, we can calculate the number of cups of punch by dividing  $4800 \div 300 = 16$  cups.

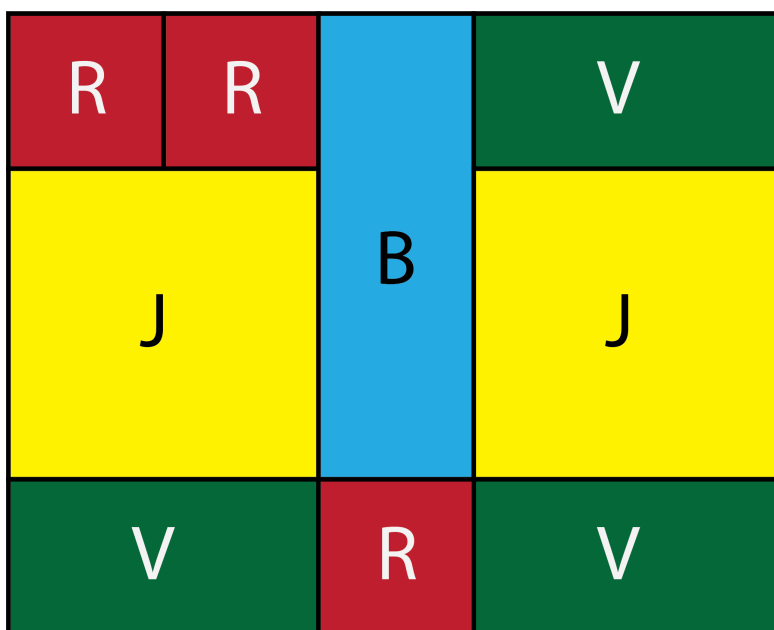


## Problème de la semaine

### Problème A

#### Des tuiles difficiles

Arvin a des tuiles rouges, jaunes, vertes et bleues. Les tuiles rouges et jaunes sont des carrés tandis que les tuiles vertes et bleues sont des rectangles. Toutes les tuiles de même couleur sont également de mêmes dimensions. Arvin place ses tuiles les unes à côté des autres de manière à former le rectangle ci-dessous.



Si Arvin voulait utiliser uniquement des carrés rouges pour former un rectangle ayant les mêmes dimensions, combien de carrés rouges lui faudrait-il?



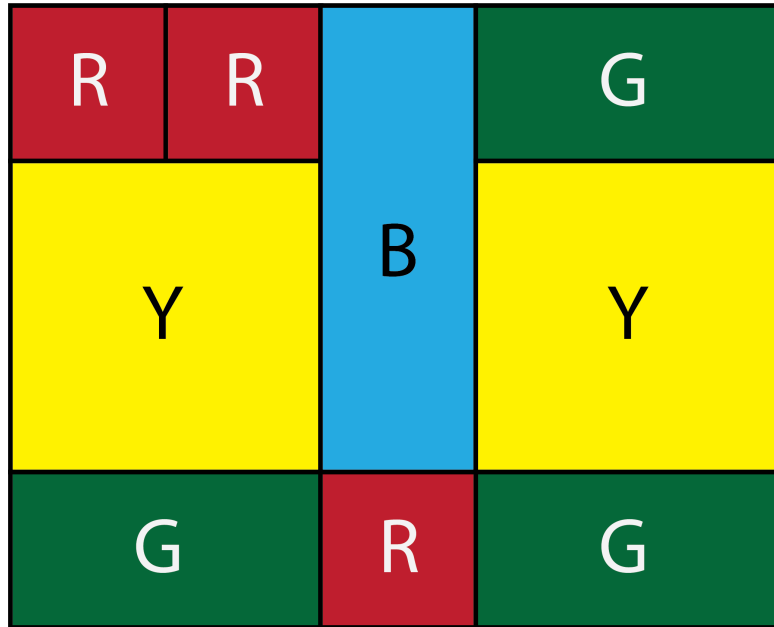
## Problem of the Week

### Problem A and Solution

#### Tricky Tiles

#### Problem

Arvin has red, yellow, green, and blue tiles. The red and yellow tiles are squares, and the green and blue tiles are rectangles. All tiles of the same colour have the same dimensions. Arvin places his tiles next to each other in order to create the following rectangle.



If Arvin wanted to use only red squares to make a rectangle with the same dimensions, how many red squares would he need?

#### Solution

We can see from the diagram that the side length of a yellow square is twice the side length of a red square. This means that if we arrange four red squares, two across and two down, we will form a square with the same dimensions as a yellow square.

We also see from the diagram that the shorter side of a green rectangle is the same length as the side length a red square, and the longer side of a green rectangle is the same length as the side length of a yellow square. Since the side length of a yellow square is twice the side length of a red square, if we arrange two red squares beside each other, we will form a rectangle with the same dimensions as a green rectangle.

From the diagram we see that the shorter side of a blue rectangle is the same length as the side length a red square, and the longer side of a blue rectangle is





the same length as the sum of the side length of a yellow square plus the side length of a red square. Since the side length of a yellow square is twice the side length of a red square, if we arrange three red squares in a line, we will form a rectangle with the same dimensions as a blue rectangle.

In summary:

- 1 yellow square = 4 red squares
- 1 green rectangle = 2 red squares
- 1 blue rectangle = 3 red squares

We can create a rectangle with the same dimensions as shown in the diagram by replacing each yellow, green, and blue tile with the equivalent number of red squares.

Tile Colour	Number in Diagram	Equivalent Number of Red Squares
yellow	2	$2 \times 4 = 8$
green	3	$3 \times 2 = 6$
blue	1	$1 \times 3 = 3$

Including the three red squares in the original diagram, we see that the rectangle can be formed using  $8 + 6 + 3 + 3 = 20$  red squares.

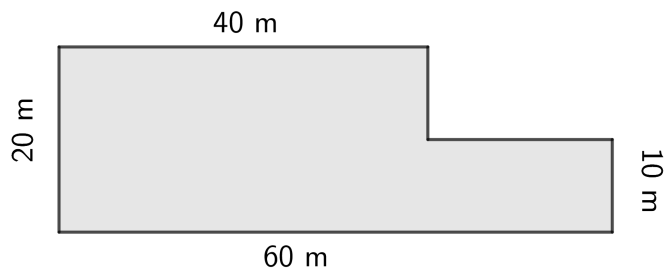


## Problème de la semaine

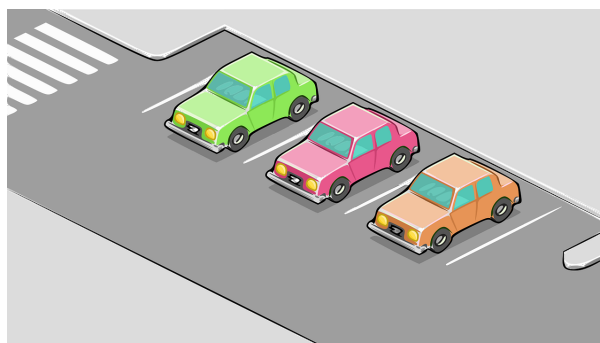
### Problème A

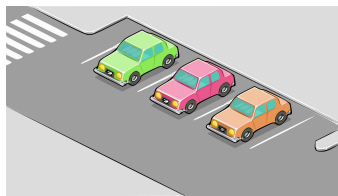
#### Le périmètre et l'aire

Dans la figure ci-dessous, on voit un parc de stationnement en forme de L ainsi que quelques-unes de ses dimensions. Tous les angles dans la figure sont des angles droits.



- (a) Quel est le périmètre du parc de stationnement?
- (b) Quelle est l'aire du parc de stationnement?





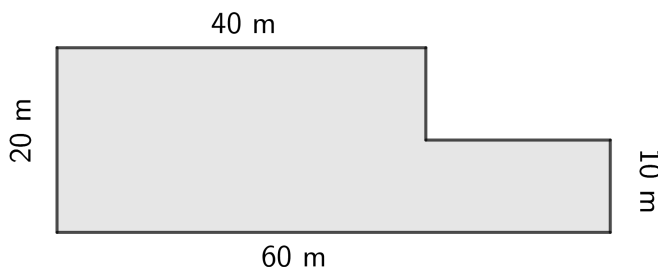
## Problem of the Week

### Problem A and Solution

#### Perimeter and Area

#### Problem

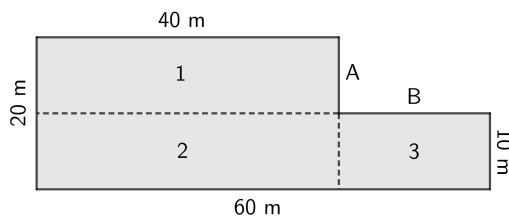
The diagram below shows the shape, and some of the dimensions, of an L-shaped parking lot. All angles in the diagram are right angles.



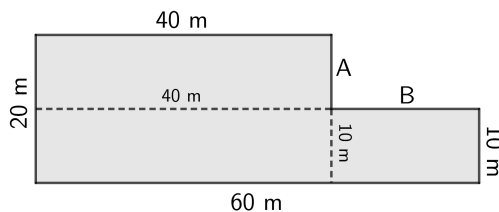
- (a) What is the perimeter of the parking lot?
- (b) What is the area of the parking lot?

#### Solution

To determine the perimeter and area of the parking lot, we add two dashed lines that extend the sides labelled A and B below. This divides the L-shaped lot into three rectangles, labelled 1, 2, and 3, as shown below.

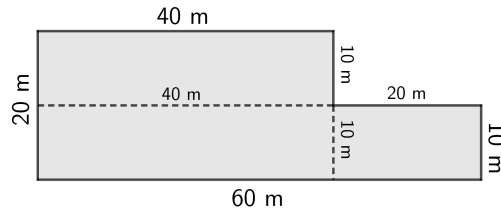


Since all angles are right angles, we know that the dashed line that is an extension of side B is 40 m in length, and the dashed line that is an extension of side A is 10 m in length.





We can now see that the length of side A is  $20 - 10 = 10$  m, and the length of side B is  $60 - 40 = 20$  m. A diagram with all of these dimensions included is shown below.



We now have enough information to calculate the perimeter and area of the parking lot.

(a) The perimeter of the parking lot is  $20 + 40 + 10 + 20 + 10 + 60 = 160$  m.

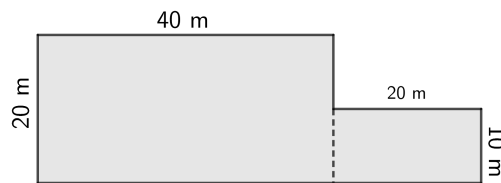
(b) The area of the parking lot is equal to the sum of the areas of the three rectangles, rectangles 1, 2, and 3.

Rectangles 1 and 2 are each 40 m by 10 m. Therefore, rectangles 1 and 2 each have an area of  $40 \times 10 = 400$  m<sup>2</sup>.

Rectangle 3 is 20 m by 10 m. Therefore, rectangle 3 has an area of  $20 \times 10 = 200$  m<sup>2</sup>.

Therefore, the total area of the parking lot is  $400 + 400 + 200 = 1000$  m<sup>2</sup>.

Alternatively, we could divide the diagram into two parts, a 40 m by 20 m rectangle and a 20 m by 10 m rectangle.



The area of the 40 m by 20 m rectangle is  $40 \times 20 = 800$  m<sup>2</sup>.

The area of the 20 m by 10 m rectangle is  $20 \times 10 = 200$  m<sup>2</sup>.

Therefore, the total area of the parking lot is  $800 + 200 = 1000$  m<sup>2</sup>.



## Problème de la semaine

### Problème A

#### Être aux petits oiseaux

Le tableau suivant présente quelques informations sur certains des plus grands oiseaux du monde. Toutefois, le tableau est incomplet.

Oiseau	Taille moyenne (en cm)
Cygne muet	
Autruche	
Manchot royal	92
Condor des Andes	
Émeu	
Casoar à casque	155
Albatros hurleur	

- (a) Utilise les informations suivantes quant aux tailles moyennes des oiseaux pour remplir le restant du tableau:
- Le condor des Andes mesure 18 cm de plus que le manchot royal.
  - Le cygne muet mesure 55 cm de moins que le casoar à casque.
  - L'albatros hurleur mesure 7 cm de plus que le cygne muet.
  - L'autruche mesure 1 m de plus que le condor des Andes.
  - Le casoar à casque mesure 20 mm de plus que l'émeu.
- (b) Classe les oiseaux selon leur taille du plus petit au plus grand.



## Problem of the Week

### Problem A and Solution

### Going to the Birds

#### Problem

The following table shows some information about some of the world's tallest birds. However, the table is incomplete.

Bird	Average Height (in cm)
Mute Swan	
Ostrich	
King Penguin	92
Andean Condor	
Emu	
Southern Cassowary	155
Wandering Albatross	

- (a) Use the following information about the average heights of these birds to fill in the rest of the table:
- The Andean Condor is 18 cm taller than the King Penguin.
  - The Mute Swan is 55 cm shorter than the Southern Cassowary.
  - The Wandering Albatross is 7 cm taller than the Mute Swan.
  - The Ostrich is 1 m taller than the Andean Condor.
  - The Southern Cassowary is 20 mm taller than the Emu.
- (b) List the birds in order from shortest to tallest.

**Solution**

- (a) Since the Andean Condor is 18 cm taller than the King Penguin, the Andean Condor is  $92 + 18 = 110$  cm tall.

Since the Mute Swan is 55 cm shorter than the Southern Cassowary, the Mute Swan is  $155 - 55 = 100$  cm tall.

Since the Wandering Albatross is 7 cm taller than the Mute Swan, the Wandering Albatross is  $100 + 7 = 107$  cm tall.

Since the Ostrich is 1 m taller than the Andean Condor, and  $1 \text{ m} = 100 \text{ cm}$ , the Ostrich is  $110 + 100 = 210$  cm tall.

Since the Southern Cassowary is 20 mm taller than the Emu, and  $20 \text{ mm} = 2 \text{ cm}$ , the Emu is  $155 - 2 = 153$  cm tall.

The completed version of the table is:

<b>Bird</b>	<b>Average Height (in cm)</b>
Mute Swan	100
Ostrich	210
King Penguin	92
Andean Condor	110
Emu	153
Southern Cassowary	155
Wandering Albatross	107

- (b) We can rank the birds from shortest to tallest using the completed table from part (a). From shortest to tallest, the birds are:  
King Penguin, Mute Swan, Wandering Albatross, Andean Condor, Emu, Southern Cassowary, Ostrich



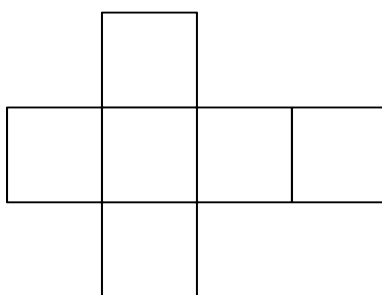
## Problème de la semaine

### Problème A

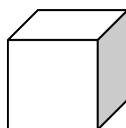
#### Les développements de Dominique

Lorsque Dominique recycle des boîtes de cartons, il les aplatit. Puisqu'il étudie les développements à l'école, il remarque qu'il existe de nombreuses façons d'aplatir une boîte en forme de cube pour en faire un développement.

Un développement est un motif qui peut être découpé puis plié pour créer une forme en 3D. Considère par exemple le développement ci-dessous.



Lorsque le développement est assemblé, il forme un cube.



En dessinant tous les développements possibles du cube, Dominique constate qu'il en existe onze différents. Dessine autant de développements que tu le peux. Arrives-tu à tous les dessiner?







## Problem of the Week

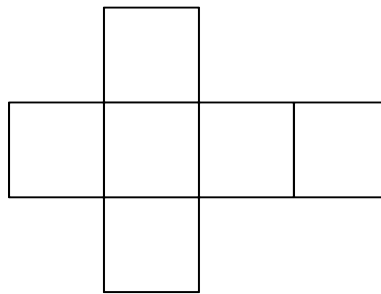
### Problem A and Solution

#### Navid's Nets

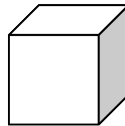
#### Problem

When Navid recycles boxes, he flattens them. Since he is learning about nets in school, he notices there are many different ways to flatten a cube-shaped box into a net.

A net is a pattern that can be cut out and then folded together to create a 3D shape. For example, consider the net shown.



When the net is folded together, it makes a cube.

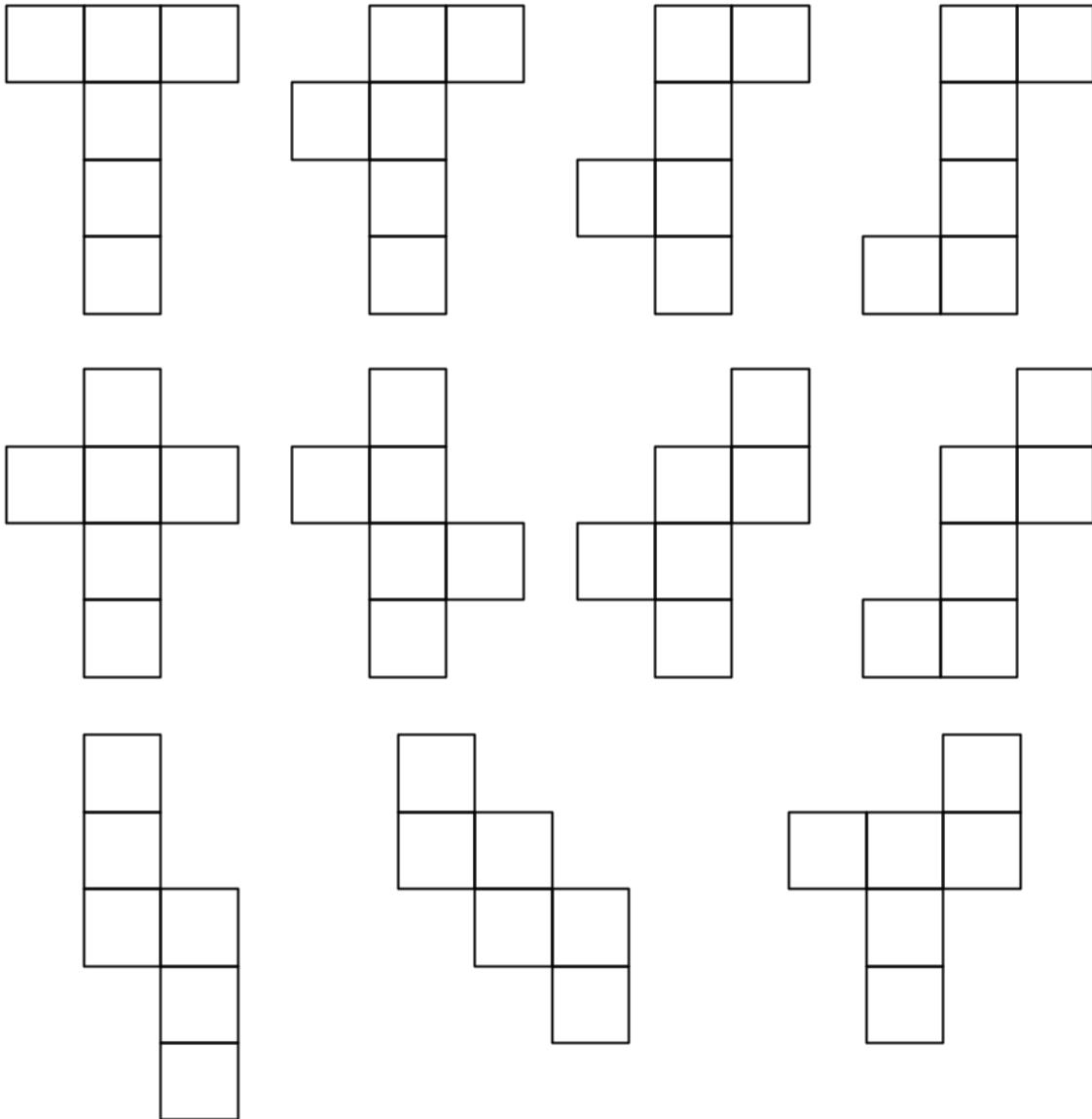


Navid draws all the possible nets for a cube and finds that there are eleven different nets. Draw as many of the nets as you can. Can you draw them all?



## Solution

The eleven possible nets for a cube are shown. Note that the nets are all considered different because for each net, flipping or rotating the net does not produce any of the other nets.





## Problème de la semaine

### Problème A

#### Jouer à la balle

Laure adore jouer à la balle avec son chien Spencer. Avant que Laure ne lance la balle, Spencer est positionné à côté d'elle. Lorsque Laure lance la balle, Spencer court vers la balle et la ramène à Laure. Laure lance la balle trois fois.

- La première fois, Laure lance la balle à une distance de 8 mètres.
- La deuxième fois, elle lance la balle deux fois plus loin que la première fois.
- La troisième fois, elle lance la balle 5 mètres moins loin que la deuxième fois.

Quelle distance Spencer a-t-il parcourue en tout?





## Problem of the Week

### Problem A and Solution

#### Playing Fetch

#### Problem

Leslie loves playing fetch with her dog Spencer. Spencer always starts by sitting beside Leslie before Leslie throws the ball. When Leslie throws the ball, Spencer runs to it and brings the ball back to the same spot. Leslie throws the ball three times.

- The first time she throws it 8 metres.
- The second time she throws it twice as far as the first time.
- The third time she throws it 5 metres less than the second time.

How far does Spencer run in total?

#### Solution

On the first throw, Spencer runs  $2 \times 8 = 16$  metres.

The distance of the second throw is  $8 \times 2 = 16$  metres.

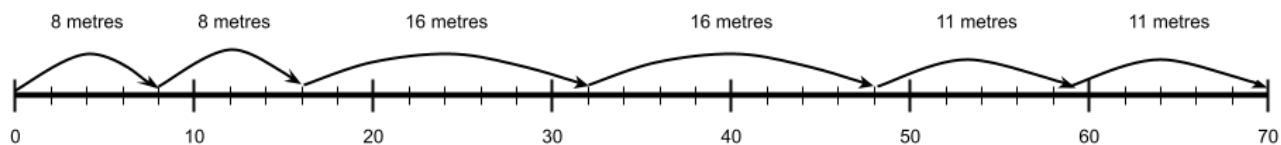
On the second throw, Spencer runs  $2 \times 16 = 32$  metres.

The distance of the third throw is  $16 - 5 = 11$  metres.

On the third throw, Spencer runs  $2 \times 11 = 22$  metres.

The total distance Spencer runs is:  $16 + 32 + 22 = 70$  metres.

We can also show the distance Spencer runs on a number line.



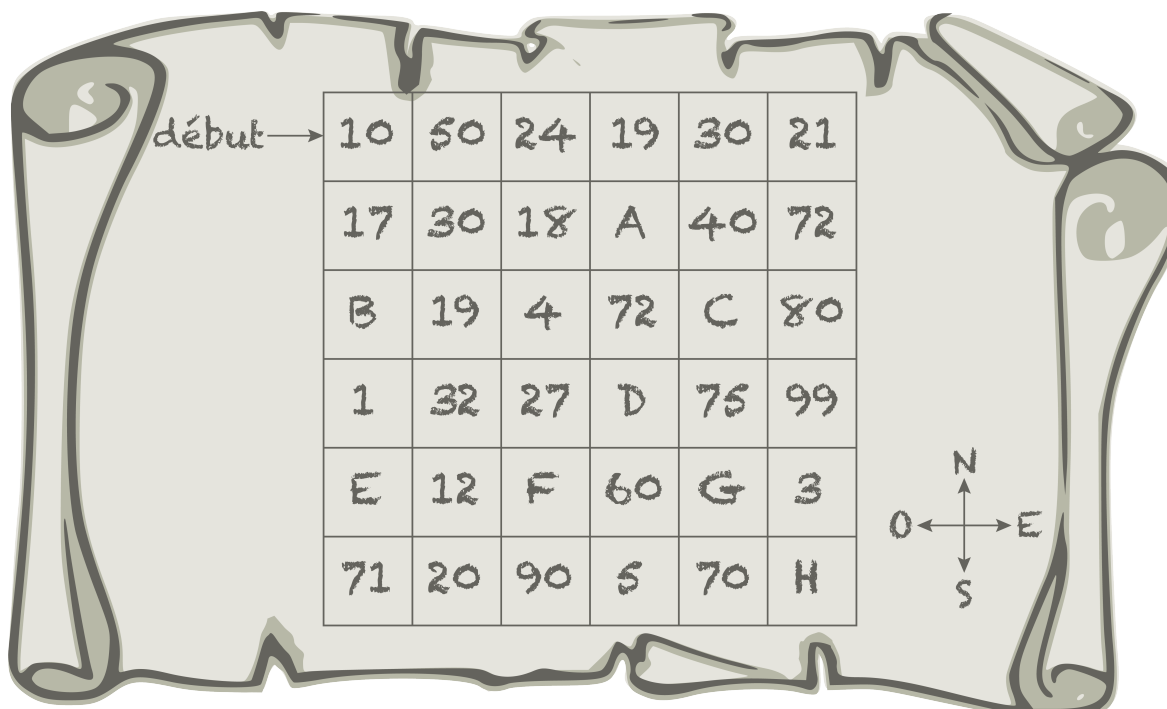


## Problème de la semaine

### Problème A

#### La carte au trésor

Robbie a trouvé une carte au trésor qui contient une grille remplie de nombres et de lettres.



La chasse au trésor commence dans le coin nord-ouest de la carte sur la case qui contient le nombre 10. Les cases contenant des nombres déterminent la direction à prendre selon les règles suivantes.

- Si le nombre est pair et un multiple de 5, déplace-toi d'une case vers l'est.
- Si le nombre est pair mais n'est pas un multiple de 5, déplace-toi d'une case vers le sud.
- Si le nombre est un multiple de 5 mais n'est pas pair, déplace-toi d'une case vers le nord.
- Si le nombre n'est ni pair ni un multiple de 5, déplace-toi d'une case vers l'ouest.

Les cases contenant des lettres représentent les emplacements possibles du trésor. Si Robbie suit les règles, il suivra un chemin qui le conduira à une case contenant une lettre. Cette case est l'endroit où est caché le trésor. À quel endroit le trésor est-il caché?

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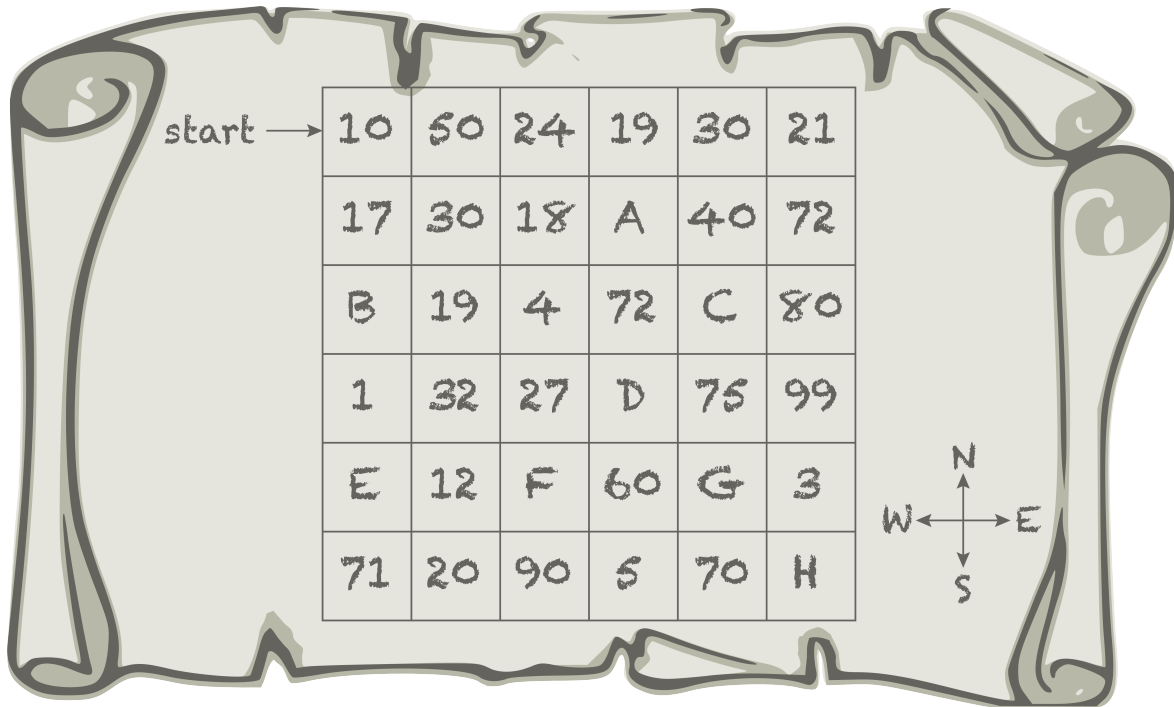
## Problem of the Week

### Problem A and Solution

#### Treasure Map

#### Problem

Robbie found a treasure map that contains a grid filled with numbers and letters.



The treasure hunt starts in the northwest corner of the grid, on the square that contains the number 10. The squares with numbers are used to determine which way to go, using the following rules.

- If the number is even and a multiple of 5, then move one square east.
- If the number is even, but not a multiple of 5, then move one square south.
- If the number is a multiple of 5, but not even, then move one square north.
- If the number is neither even nor a multiple of 5, then move one square west.

The squares with letters represent possible locations of the treasure. If Robbie follows the rules, he will follow a path that reaches a square with a letter, which is where the treasure is hidden. Where is the treasure hidden?

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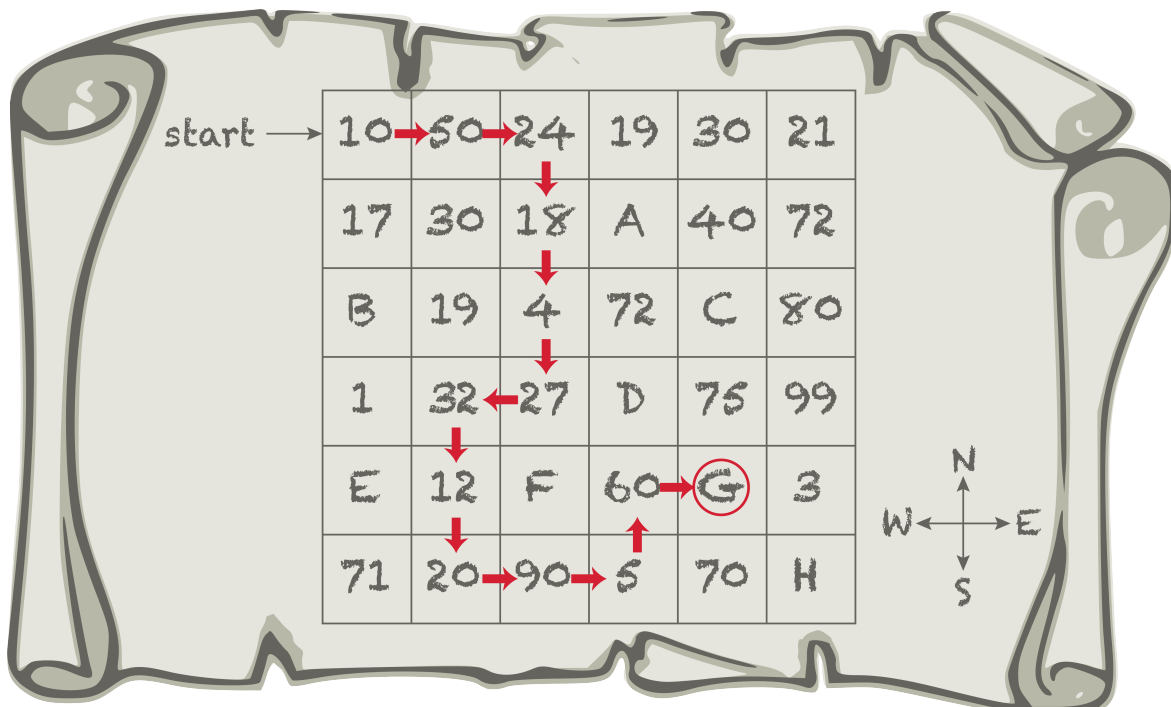


### Solution

Starting in the northwest corner of the map, here are the steps Robbie would follow to find the hidden treasure.

- 10 is an even number and a multiple of 5, so move one square east.
- 50 is an even number and a multiple of 5, so move one square east again.
- 24 is an even number but not a multiple of 5, so move one square south.
- 18 is an even number but not a multiple of 5, so move one square south again.
- 4 is an even number but not a multiple of 5, so move one square south again.
- 27 is neither even nor a multiple of 5, so move one square west.
- 32 is an even number but not a multiple of 5, so move one square south.
- 12 is an even number but not a multiple of 5, so move one square south again.
- 20 is an even number and a multiple of 5, so move one square east.
- 90 is an even number and a multiple of 5, so move one square east again.
- 5 is a multiple of 5 but not an even number, so move one square north.
- 60 is an even number and a multiple of 5, so move one square east.
- Robbie has reached a square with a letter, so the treasure is hidden in location G.

The path to the hidden treasure is shown on the map below.



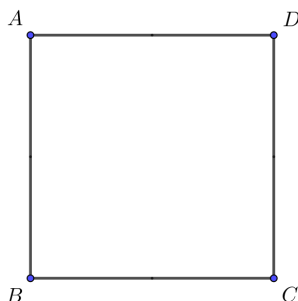


## Problème de la semaine

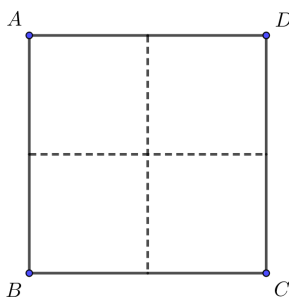
### Problème A

#### Origami

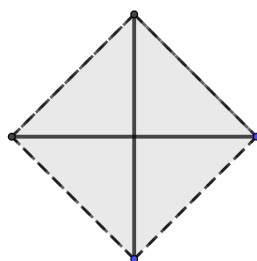
Laila commence avec une feuille de papier carrée. En commençant par un coin et en se déplaçant autour du carré, elle nomme les coins  $A$ ,  $B$ ,  $C$  et  $D$ .



Laila plie le papier en deux, en repliant le côté  $AB$  sur le côté  $DC$  de manière à former un rectangle. Elle déplie le papier et le plie à nouveau, cette fois-ci en pliant le côté  $AD$  sur le côté  $BC$ , de manière à former un autre rectangle. Lorsqu'elle déplie le papier à nouveau, elle voit deux plis dans le papier, comme dans la figure ci-dessous.



Le centre du carré est le point où les deux plis se coupent. Ensuite, elle prend chaque coin du carré et plie le papier de manière que chacun des coins touche le centre du carré. En pliant les quatre coins de cette manière, elle obtient un autre carré plus petit composé de quatre régions triangulaires, comme dans la figure ci-dessous.



Quelle fraction de l'aire du grand carré original représente l'aire du petit carré? Justifie ta réponse.





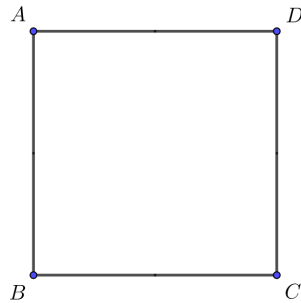
# Problem of the Week

## Problem A and Solution

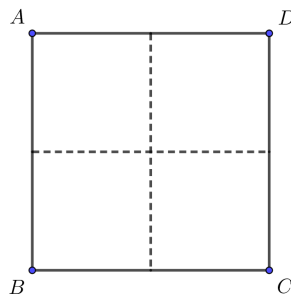
### Origami

#### Problem

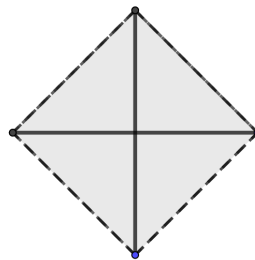
Laila starts with a square piece of paper. Starting at one corner and moving around the square, she labels the corners  $A$ ,  $B$ ,  $C$ , and  $D$ .



Laila folds the paper in half, by folding side  $AB$  onto side  $DC$ , to form a rectangle. She opens up the paper and folds it again to form another rectangle by folding side  $AD$  onto side  $BC$ . When she opens up the paper this time, she sees two creases in the paper as shown below.



The centre of the square is the point where the two creases intersect. Now, she takes each corner of the square and folds the paper so that each corner touches the centre of the square. Folding all four corners in this way forms another smaller square made up of four triangular regions as shown below.



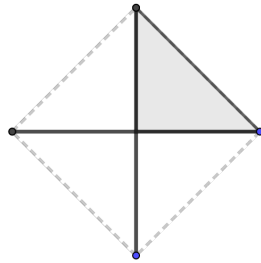
What fraction of the area of the original square is the area of this smaller square? Justify your answer.



### Solution

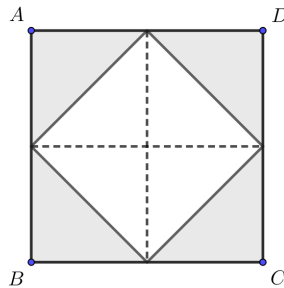
The smaller square has an area that is  $\frac{1}{2}$  the area of the original square. A justification of this is given below.

Consider the following image of the smaller square with only one of the four triangular regions shaded.



Underneath the shaded triangle is a region of the original square that is exactly the same size. That is true for all four of the triangles that were formed by having the corners meet at the centre of the original square.

Let's now shade all four of the triangular regions in the smaller square, and then open up the paper again.



We can make the following observations:

- The shaded triangles each have a matching unshaded triangle.
- The shaded triangles make up the area of the smaller square.
- The area of the original square is equal to the area of the shaded triangles plus the area of the smaller square. This means the area of the original square is 2 times the area of the smaller square.

It follows that the area of the smaller square is  $\frac{1}{2}$  the area of the original square.



## Problème de la semaine

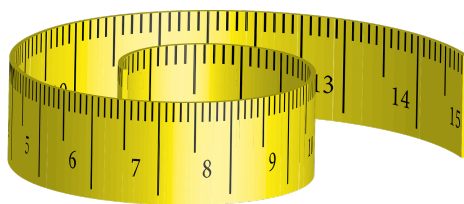
### Problème A

#### Mesurez-moi

Arezoo, Femke, Jackson, Nya et Élisabeth ont créé un tableau dans lequel ils ont inscrit leurs tailles à différents âges de leur vie.

Nom	Taille à la naissance	Taille à l'âge de 6 ans	Taille adulte
Arezoo	44 cm	106 cm	1,51 m
Femke	47 cm	104 cm	153 cm
Jackson	49 cm	108 cm	2 m
Nya	48 cm	1,11 m	189 cm
Élisabeth	52 cm	1 m et 19 cm	1,84 m

- (a) Qui a le plus grandi entre la naissance et l'âge de 6 ans ? Qui a le moins grandi entre la naissance et l'âge de 6 ans ? Justifie tes réponses.
- (b) À l'aide de l'estimation, écris la liste d'amis en ordre croissant de croissances (soit de la croissance la moins élevée à la croissance la plus élevée) entre l'âge de 6 ans et l'âge adulte.





## Problem of the Week

### Problem A and Solution

#### Measure Me

#### Problem

Arezoo, Femke, Jackson, Nya, and Elisabeth made a table that recorded their heights at different stages of their lives.

Name	Height at Birth	Height at Age 6	Adult Height
Arezoo	44 cm	106 cm	1.51 m
Femke	47 cm	104 cm	153 cm
Jackson	49 cm	108 cm	2 m
Nya	48 cm	1.11 m	189 cm
Elisabeth	52 cm	1 m and 19 cm	1.84 m

- (a) Who grew the most between birth and age 6? Who grew the least between birth and age 6? Justify your answers.
- (b) Using estimation, arrange the list of friends from least growth to most growth from age 6 to adulthood.

#### Solution

- (a) One way to solve this is to convert all of the measurements into centimetres and then find the difference between each person's height at age 6 and at birth.

Name	Height at Birth	Height at Age 6	Height Difference
Arezoo	44 cm	106 cm	$106 - 44 = 62$ cm
Femke	47 cm	104 cm	$104 - 47 = 57$ cm
Jackson	49 cm	108 cm	$108 - 49 = 59$ cm
Nya	48 cm	111 cm	$111 - 48 = 63$ cm
Elisabeth	52 cm	119 cm	$119 - 52 = 67$ cm

Elisabeth grew the most between birth and age 6.  
Femke grew the least between birth and age 6.



- (b) We will estimate the growth of each person by rounding numbers to the nearest 10 cm.

Name	Approximate Height at Age 6	Approximate Adult Height	Approximate Difference
Arezoo	110 cm	150 cm	$150 - 110 = 40$ cm
Femke	100 cm	150 cm	$150 - 100 = 50$ cm
Jackson	110 cm	200 cm	$200 - 110 = 90$ cm
Nya	110 cm	190 cm	$190 - 110 = 80$ cm
Elisabeth	120 cm	180 cm	$180 - 120 = 60$ cm

When we list the friends in order by approximate growth between age 6 and adulthood, from least growth to most growth, we get:

Arezoo, Femke, Elisabeth, Nya, and Jackson

It turns out that if we determine the actual difference between each person's adult height and height at age 6, and then list the friends in order from least growth to most growth, we would get the same ordering. However, this will not always be the case. For example, if Arezoo's adult height had been 1.54 m and Femke's adult height had been 151 cm, then the order when approximating would have been the same as above, but the actual order would have been Femke, Arezoo, Elisabeth, Nya, Jackson.

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# Algèbre (A)

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## Problème de la semaine

### Problème A

### Épreuve de relais

Lors d'un concours international, des équipes venant des quatre coins du monde ont disputé une épreuve de relais. Ce type d'épreuve est disputé par équipe de quatre concurrents. Selon les règles de l'épreuve, chaque concurrent doit avancer en bondissant et le passage du relais se fait au moyen d'un contact physique entre les relayeurs. En d'autres mots, le premier membre de chaque équipe commence l'épreuve et avance en bondissant jusqu'à ce qu'il touche le membre suivant de son équipe. Ce dernier avance en bondissant vers le prochain membre de son équipe et le touche pour passer le relais, et ainsi de suite, jusqu'à ce que le relais passe au dernier membre de l'équipe (ce dernier avancera en bondissant vers la ligne d'arrivée).

Lucky le Lapin et Kicky le Kangourou sont dans des équipes différentes et bondiront chacun dans la dernière étape de la course. Chacun d'eux est situé à 24 m de la ligne d'arrivée et attend que son coéquipier lui passe le relais.

Le coéquipier de Lucky le Lapin l'atteint en premier et lui passe le relais. Lucky le Lapin bondit trois fois avant que Kicky le Kangourou ne commence à avancer. Donc, le quatrième bond de Lucky et le premier bond de Kicky ont lieu en même temps. Lucky le Lapin avance de 2 m à chaque bond tandis que Kicky le Kangourou avance de 3 m à chaque bond. De plus, les deux animaux sautent et atterrissent en même temps à chaque bond.

- Quel animal atteindra la ligne d'arrivée en premier ? Justifie ta réponse.
- Est-ce que les deux animaux vont parfois atterrir au même endroit (pas nécessairement en même temps)? Si oui, à quelle distance de la ligne d'arrivée se trouvent ces endroits?





## Problem of the Week

### Problem A and Solution

### International Jumping Relay

#### Problem

The International Jumping Relay Race will take place this year. In the race, each team has four members. The first member of each team starts the race and jumps until they tag the next member of their team. When a team member is tagged, they start jumping towards the next team member to tag them, except for the last team member who starts jumping towards the finish line.

BeHappy Bunny and Kicky Kangaroo are on different teams and will each be jumping in the last leg of the race. They are waiting 24 m away from the finish line for their teammates to tag them.

BeHappy Bunny is tagged first, and jumps three times before Kicky Kangaroo is tagged. Bunny's fourth jump and Kangaroo's first jump happen at the same time. BeHappy Bunny leaps 2 m forward with every jump, Kicky Kangaroo leaps 3 m forward with every jump, and the two animals take off and land at the same time on each jump.

- (a) Which animal will get to the finish line first? Justify your answer.
- (b) Will the two animals ever land at the same spot (not necessarily at the same time)? If so, how far away from the finish line are these spots?

#### Solution

One way to solve this problem is to make a table that keeps track of how far each animal has travelled after each jump. Recall that BeHappy Bunny jumps three times before Kicky Kangaroo jumps for the first time.

Bunny's Jump Number	Distance Jumped by Bunny (m)	Distance Jumped by Kangaroo (m)
1	2	0
2	4	0
3	6	0
4	8	3
5	10	6
6	12	9
7	14	12
8	16	15
9	18	18
10	20	21
11	22	24
12	24	27





- (a) Based on the table, we see that Kicky Kangaroo will get to the finish line, which is 24 m away, on Bunny's 11<sup>th</sup> jump. Bunny will get to the finish line on their 12<sup>th</sup> jump. So Kicky Kangaroo will get to the finish line first.

Another way to determine the winner is to see how many jumps it takes for each to travel 24 m. We can do this with division:

BeHappy Bunny will take  $24 \div 2 = 12$  jumps to get to the finish line.

Kicky Kangaroo will take  $24 \div 3 = 8$  jumps to get to the finish line.

Since BeHappy Bunny jumps three times before Kicky Kangaroo starts, we can say that Bunny takes  $12 - 3 = 9$  jumps to get to the finish line from the time that Kangaroo starts jumping. However, this is one more jump than it takes Kangaroo to get to the finish line. So Kicky Kangaroo will get to the finish line first.

- (b) There are four spots where both animals will land. These are exactly 6 m, 12 m, 18 m, and 24 m from where the animals were waiting to be tagged. (Notice that these numbers are all common multiples of 2 and 3, which represent each animal's jumping distance.)

Therefore, the spots where they both land are  $24 - 6 = 18$  m,

$24 - 12 = 12$  m,  $24 - 18 = 6$  m, and  $24 - 24 = 0$  m from the finish line.



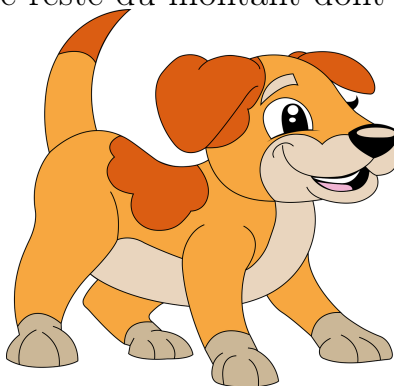
## Problème de la semaine

### Problème A

#### Adopter un chien

Robbie veut adopter un chien. Il décide de contribuer aux dépenses essentielles. Il veut faire un don de 60 \$ au refuge pour animaux d'où il pense adopter son chien. De plus, il compte participer à l'achat de la nourriture pour chiens à raison de 10 \$ par mois.

- (a) En tout, combien lui coûtera l'adoption et la nourriture pour chiens pendant la première année?
- (b) Robbie doit économiser le montant calculé dans la partie (a) avant d'adopter le chien. Il a 87 \$ dans sa tirelire. Il reçoit une allocation de 7 \$ chaque semaine pour avoir fait ses tâches ménagères. Combien de temps lui faudra-t-il pour gagner le reste du montant dont il a besoin?





## Problem of the Week

### Problem A and Solution

#### Puppy Plans

#### Problem

Robbie wants to get a puppy, so he decides to help pay the costs. He wants to donate \$60 to the animal shelter he gets the puppy from, and he needs to contribute \$10 every month to help buy the puppy's food.

- How much money does Robbie need to help pay the cost of getting the puppy and feeding the puppy in the first year?
- Robbie needs to save the money calculated in part (a) before getting the puppy. He has \$87 in his piggy bank. He earns a \$7 allowance every week for doing his chores. How long will it take Robbie to earn the rest of the money he needs?

#### Solution

- Since there are 12 months in a year and Robbie wants to contribute \$10 each month, he needs  $12 \times 10 = \$120$  for puppy food in the first year. Counting the shelter donation, Robbie needs  $\$60 + \$120 = \$180$  in total.
- We can make a table to calculate how long it will take for Robbie to save enough money to have at least \$180. He starts with \$87 and will increase his total by \$7 each week.

Week	Total Saved (in \$)
0	87
1	94
2	101
3	108
4	115
5	122
6	129
7	136
8	143
9	150
10	157
11	164
12	171
13	178
14	185

So it will take Robbie 14 weeks to earn enough money to help cover the shelter donation and the costs of feeding the puppy in the first year.

Alternatively, since Robbie has already saved \$87, he needs to earn  $\$180 - \$87 = \$93$  more. We calculate how long it will take to earn the remaining amount using division.

Since  $93 \div 7 = 13$  with a remainder of 2, we round up to determine that it will take 14 weeks to earn the additional \$93 Robbie needs.



## Problème de la semaine

### Problème A

#### Calculs de boîtes noires

Le CEMI a créé des boîtes noires qui transforment des nombres. Les machines acceptent un nombre comme entrée, effectuent des calculs sur ce nombre, puis produisent une sortie.

Ronit a configuré sa boîte noire pour qu'elle multiplie d'abord l'entrée par 2, puis qu'elle ajoute 8 à ce résultat.



Par exemple, si Ronit introduit le nombre 10 comme entrée, sa boîte noire multiplierait d'abord ce nombre par 2 pour obtenir 20. Ensuite, elle ajouterait 8 à ce nombre pour produire une sortie finale de 28.

Amrita a configuré sa boîte noire pour qu'elle multiplie d'abord l'entrée par 4, puis qu'elle soustrait 6 de ce résultat.



- Si Amrita introduit le nombre 10 comme entrée, quel nombre la machine produira-t-elle comme sortie?
- Ronit et Amrita ont le même âge et ont plus de 3 ans. S'ils introduisent chacun leur âge comme entrée dans leur boîte noire, ils obtiennent tous deux la même sortie. Quel âge ont-ils ?
- Écris deux configurations de boîtes noires ayant 10 comme entrée et 16 comme sortie. Tu peux utiliser n'importe quelles deux opérations parmi les suivantes: addition, soustraction, multiplication ou division.



## Problem of the Week

### Problem A and Solution

#### Black Box Calculations

#### Problem

The CEMC has created black box machines that process numbers. The machines accept an input number, then do calculations based on that number, then produce an output.

Ronit set up his black box machine to first multiply the input number by 2, and then add 8 to the result.



For example, if Ronit inputs the number 10, his black box machine will first multiply it by 2 to produce the number 20. Then it will take the number 20 and add 8 to produce the final output of 28.

Amrita set up her black box machine to first multiply the input number by 4, and then subtract 6 from the result.



- Amrita inputs the number 10 into her black box machine. What number will the machine output?
- Ronit and Amrita are the same age and they are older than 3. They each put their age number into their black box machine and were surprised to get the same output as each other. How old are Ronit and Amrita?
- Write two black box machine setups that have an input of 10 and an output of 16. You can use any two of the following operations: addition, subtraction, multiplication, or division.

**Solution**

- (a) If Amrita inputs the number 10, the black box machine will first multiply it by 4 to produce the number 40. Then it will take the number 40 and subtract 6 to produce the final output of 34. So her black box machine will output 34.
- (b) One way to solve this problem is to create a table for each machine and keep track of the output produced for different inputs, starting at 4.

**Ronit's Machine**

Input	Result after multiplying by 2	Result after adding 8	Output
4	$4 \times 2 = 8$	$8 + 8 = 16$	16
5	$5 \times 2 = 10$	$10 + 8 = 18$	18
6	$6 \times 2 = 12$	$12 + 8 = 20$	20
7	$7 \times 2 = 14$	$14 + 8 = 22$	22

**Amrita's Machine**

Input	Result after multiplying by 4	Result after subtracting 6	Output
4	$4 \times 4 = 16$	$16 - 6 = 10$	10
5	$5 \times 4 = 20$	$20 - 6 = 14$	14
6	$6 \times 4 = 24$	$24 - 6 = 18$	18
7	$7 \times 4 = 28$	$28 - 6 = 22$	22

From these tables we see that when the input is 7, the output is 22 for both machines. So one possibility is that Ronit and Amrita are 7 years old.

Is it possible that Ronit and Amrita are a different age? Looking at the Output columns in the tables, we see that the output from Ronit's black box machine increases by 2 as the input increases by 1. However, the output from Amrita's black box machine increases by 4 as the input increases by 1. Since the output from Amrita's black box machine is increasing faster than the output from Ronit's black box machine, this tells us that their outputs will not be the same for any other possible ages.

So Ronit and Amrita must both be 7 years old.

- (c) There are many possible setups that would produce an output of 16 given an input of 10. Some setups are shown below.
- First divide by 5, then add 14.
  - First multiply by 2, then subtract 4.
  - First add 22, then divide by 2.
  - First subtract 2, then multiply by 2.

**EXTENSION:** We could describe the setup of each machine by writing a mathematical formula that describes the operations for the black box. The formula would use a letter such as  $n$  to represent the input number. Can you write a mathematical formula for each of the two machine setups from part (a)?









## Solution

- (a) We can make a table showing the number of stitches in each row as we follow the pattern.

Rows	Number of Stitches
1 – 6	35
7 – 12	37
13 – 18	39
19 – 24	41

Since 20 is between 19 and 24, there will be 41 stitches in the 20<sup>th</sup> row.

- (b) We can make a table showing the row number and the length of the item after that row has been knitted. Here we will use skip counting and look at the length after every 6<sup>th</sup> row.

Row	Length (in cm)
6	3
12	6
18	9
24	12
30	15
36	18
42	21
48	24
54	27
60	30

After 60 rows, our finished item will have a length of 30 cm.

- (c) We can make another table showing the number of stitches in each row, again using skip counting and looking at every 6<sup>th</sup> row up to row 60.

Row	Number of Stitches
6	35
12	37
18	39
24	41
30	43
36	45
42	47
48	49
54	51
60	53

The 60<sup>th</sup> row will have 53 stitches.



## Problème de la semaine

### Problème A

#### Décisions de données

La famille Webb essaie de se décider pour l'achat d'un nouveau plan mensuel de données Internet. Trois choix s'offrent à elle:

Plan A: 10 \$ pour les 10 premiers Go de données et 5 \$ pour chaque 2 Go supplémentaires.

Plan B: 40 \$ pour les 20 premiers Go de données et 10 \$ pour chaque 10 Go supplémentaires.

Plan C: 80 \$ pour un nombre illimité de Go de données.

Remarque que pour le plan A, les données supplémentaires doivent être achetées par tranches de 2 Go. De même, pour le plan B, les données supplémentaires doivent être achetées par tranches de 10 Go.

Sachant que la famille utilisera entre 25 et 40 Go de données chaque mois, quel plan la famille Webb devrait-elle choisir ? Justifie ta réponse.





## Problem of the Week

### Problem A and Solution

#### Deciding About Data

#### Problem

The Webb family is trying to decide on a new monthly internet plan. There are three choices:

Plan A: \$10 for the first 10 GB of data, and each additional 2 GB costs \$5.

Plan B: \$40 for the first 20 GB of data, and each additional 10 GB costs \$10.

Plan C: \$80 for unlimited GB of data.

Note that for Plan A, additional data has to be purchased in 2 GB increments. Similarly, for Plan B, additional data has to be purchased in 10 GB increments.

After keeping track of data used, the family decides they will use between 25 GB and 40 GB of data each month. Which plan should the Webb family choose? Justify your answer.

#### Solution

One way to make a decision is to make a table showing how much each plan would cost for various amounts of data use.

Data Used (in GB)	Total Cost (in \$) for Plan A	Total Cost (in \$) for Plan B	Total Cost (in \$) for Plan C
10	10	40	80
12	15	40	80
14	20	40	80
16	25	40	80
18	30	40	80
20	35	40	80
22	40	50	80
24	45	50	80
26	50	50	80
28	55	50	80
30	60	50	80
32	65	60	80
34	70	60	80
36	75	60	80
38	80	60	80
40	85	60	80

Notice that at 25 GB, with Plan A they would need to get 26 GB of data. This would cost \$50. So, comparing the cost of the plans, we notice that Plan B is the lowest price from 25 GB to 40 GB. Therefore, the family should choose Plan B.

(Note that if the family uses less than 25 GB per month, then Plan A is better. Also, if they use more than 40 GB, then it looks like Plan B is better at first, but Plan C will eventually be better.)



## Problème de la semaine

### Problème A

#### Problèmes d'aquarium

Jacques a reçu un aquarium pour son anniversaire et veut le remplir avec des guppys et des tétras. Les guppys sont vendus par groupes de quatre et les tétras par groupes de trois. Il peut acheter quatre guppys pour 12 \$ et trois tétras pour 7 \$.

Si Jacques a dépensé exactement 50 \$ pour acheter des poissons, combien de poissons de chaque type a-t-il acheté?





## Problem of the Week

### Problem A and Solution

#### Aquarium Issues

#### Problem

Jacques got an aquarium for his birthday and wants to fill it with some guppies and tetras. Guppies are sold in groups of four and tetras are sold in groups of three. He can buy four guppies for \$12, and three tetras for \$7.

If Jacques spent exactly \$50 on fish, how many of each fish did he buy?

#### Solution

Since 50 is not a multiple of 12 or a multiple of 7, then Jacques must have bought some of each fish in order to spend exactly \$50. One way to solve this problem is to make a table to keep track of how much money it costs for multiples of four guppies, and how much of the \$50 would be left to buy tetras.

Number of Guppies	Cost for Guppies (in \$)	Money Leftover for Tetras (in \$)
4	$1 \times 12 = 12$	$50 - 12 = 48$
8	$2 \times 12 = 24$	$50 - 24 = 26$
12	$3 \times 12 = 36$	$50 - 36 = 14$
16	$4 \times 12 = 48$	$50 - 48 = 2$

Now we look for a multiple of seven in the leftover money, because each group of tetras costs \$7. The only multiple of seven in the leftover money is 14. Since  $14 = 2 \times 7$ , Jacques must have bought two groups of tetras.

This means Jacques bought 12 guppies and  $2 \times 3 = 6$  tetras.



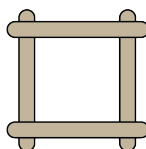
## Problème de la semaine

### Problème A

#### Construction artisanale

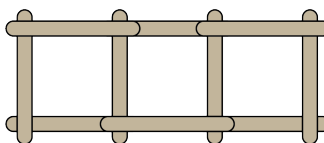
Sam fabrique des cadres photo carrés avec des bâtonnets de bois. Il a une boîte de 50 bâtonnets de bois et veut fabriquer 13 cadres.

- (a) Sam prévoit fabriquer des cadres individuels en utilisant quatre bâtonnets de bois comme dans la figure ci-dessous.



Aura-t-il assez de bâtonnets pour fabriquer 13 cadres? Justifie ta réponse.

- (b) Sam change d'avis et, au lieu de fabriquer des cadres individuels, il décide de relier les cadres en une rangée. Il commence par fabriquer un cadre à l'aide de quatre bâtonnets de bois, puis crée un deuxième cadre attaché au premier en utilisant trois bâtonnets. Il rajoute ensuite trois autres bâtonnets pour créer un troisième cadre attaché aux deux premiers, comme dans la figure ci-dessous.



Sam prévoit poursuivre ce processus, en utilisant trois bâtonnets de bois supplémentaires pour chaque cadre, jusqu'à ce qu'il ait en tout 13 cadres qui soient reliés en rangée. Aura-t-il assez de bâtonnets de bois pour fabriquer 13 cadres? Justifie ta réponse.

- (c) Peux-tu dessiner une autre disposition des 13 cadres que Sam aurait pu construire en utilisant au maximum 50 bâtonnets de bois? Combien de bâtonnets de bois as-tu utilisé dans ton dessin?
- (d) Peux-tu dessiner une disposition des 13 cadres qui contient moins de 35 bâtonnets de bois?



# Problem of the Week

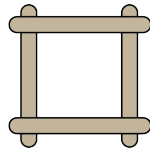
## Problem A and Solution

### Crafty Construction

#### Problem

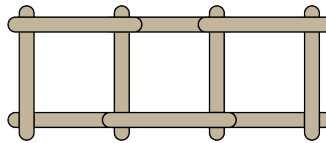
Sam is making square picture frames using popsicle sticks. He has one box of 50 popsicle sticks and wants to make 13 frames.

- (a) Sam plans to make individual frames using four popsicle sticks as shown.



Will he have enough popsicle sticks to make 13 frames? Justify your answer.

- (b) Sam changes his mind and instead of individual frames, he decides to connect the frames in a row. He starts by making a frame using four popsicle sticks, and then uses three popsicle sticks to create another frame attached to this frame. He then uses three more popsicle sticks to create another frame attached to the first two frames, so he has three connected frames, as shown.



Sam plans to continue this process, using three more popsicle sticks for each frame, until he has 13 frames connected in a row. Will he have enough popsicle sticks to make 13 frames? Justify your answer.

- (c) Can you draw another layout of the 13 frames that Sam could have built using at most 50 popsicle sticks? How many popsicle sticks does your layout use?
- (d) Can you draw a layout of the 13 frames that uses fewer than 35 popsicle sticks?



## Solution

- (a) Since each frame requires 4 popsicle sticks, the total number of popsicle sticks required for 13 frames is equal to  $13 \times 4 = 52$ .

Alternatively, we could make a table showing the number of frames and the number of popsicle sticks required.

Number of Frames	Number of Popsicle Sticks
1	4
2	8
3	12
4	16
5	20
6	24
7	28
8	32
9	36
10	40
11	44
12	48
13	52

Either way, since it will take 52 popsicle sticks to make 13 individual frames, Sam will not have enough popsicle sticks to make all the frames.

- (b) The first frame uses 4 popsicle sticks but the other 12 frames use only 3 popsicle sticks each. So the total number of popsicle sticks required can be found by adding 4 to  $12 \times 3$ . Since  $12 \times 3 = 36$ , this gives a total of  $4 + 36 = 40$  popsicle sticks.

Alternatively, we could make a table showing the number of frames and the number of popsicle sticks required.

Number of Frames	Number of Popsicle Sticks
1	4
2	7
3	10
4	13
5	16
6	19
7	22
8	25
9	28
10	31
11	34
12	37
13	40

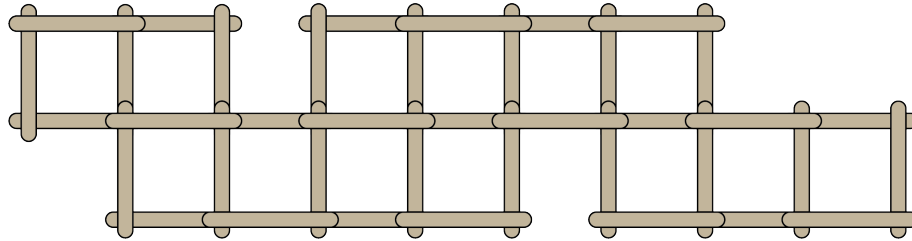
Either way, since it will take 40 popsicle sticks to build a row of 13 connected frames, Sam will have enough popsicle sticks to make all the frames.



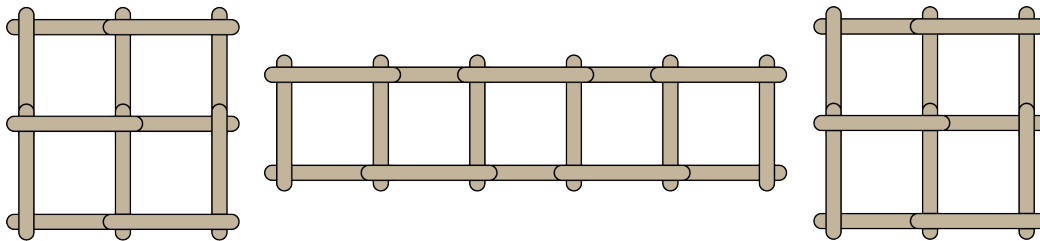


- (c) There are many layouts of 13 frames you could make using at most 50 popsicle sticks. Two examples are shown.

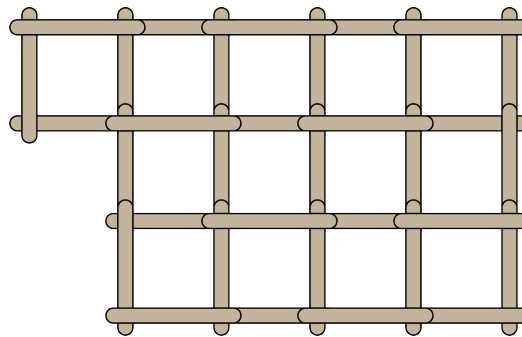
The following layout uses 39 popsicle sticks.



The following layout uses 40 popsicle sticks.



- (d) The most efficient use of popsicle sticks is to share as many sides as possible with other frames. If you connect the frames to form a shape as close as possible to a square, you can make 13 frames using only 34 popsicle sticks, as shown.



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# Gestion des données (D)

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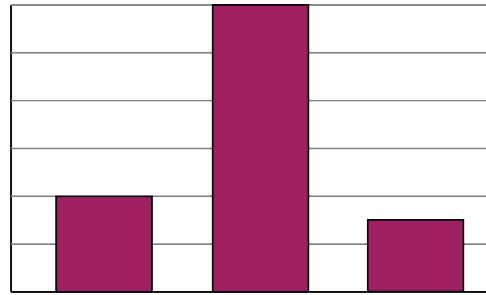
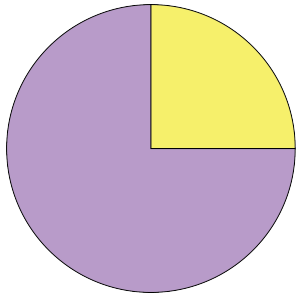


## Problème de la semaine

### Problème A

#### Des données manquantes

Jasmine a représenté les valeurs de certaines données à l'aide d'un diagramme circulaire et d'un diagramme à bandes. Or, elle a oublié quels nombres correspondaient à quel diagramme. Les diagrammes sont présentés ci-dessous. Il y a cinq valeurs au total; deux sont représentées dans le diagramme circulaire et trois sont représentées dans le diagramme à bandes.



Les valeurs des données sont: V: 30, W: 40, X: 60, Y: 120, Z: 180

Pour chaque diagramme, inscris les lettres correspondant aux valeurs appropriées. Ensuite, complète l'échelle de l'axe vertical du diagramme à bandes en y ajoutant des valeurs.



## Problem of the Week

### Problem A and Solution

#### Missing Data

#### Problem

Jasmine created a circle chart and a bar chart based on data values, but forgot what numbers went with which chart. The charts are shown below. There are five values in total, two belong to the circle chart and three belong to the bar chart.



Here are the values:

V: 30, W: 40, X: 60, Y: 120, Z: 180

Label each chart with the letters matching the appropriate values. Then add values to the scale on the vertical axis of the bar chart.

#### Solution

Comparing the size of the sections in the circle chart, we see that the smaller section appears to be one quarter of the whole circle and the larger section appears to be three quarters of the whole circle. This means the larger section is three times the size of the smaller section. Comparing the heights of the bars, we can see that the tallest bar is three times the height of the leftmost bar. We should look at the data to find pairs of numbers where one number is three times the other number.

From the values listed we see that  $3 \times 40 = 120$  and  $3 \times 60 = 180$ . So the circle chart values could be either 120 and 40 or 180 and 60.

- If the circle chart values are 120 and 40, then the remaining three values would be the bar chart values. This would mean that the tallest bar would be representing the value 180 and the leftmost bar would be representing the value 60. This means the rightmost bar would be representing the remaining value, which is 30. However, 30 is half as much as 60. This means the rightmost bar should be half the height of the leftmost bar. In the chart,

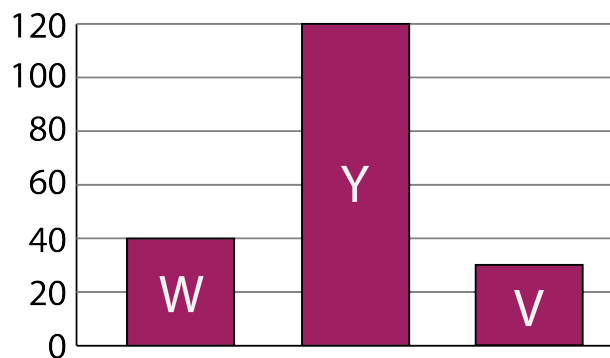


we can see that the rightmost bar is *more* than half the height of the leftmost bar. Therefore, these values cannot be correct.

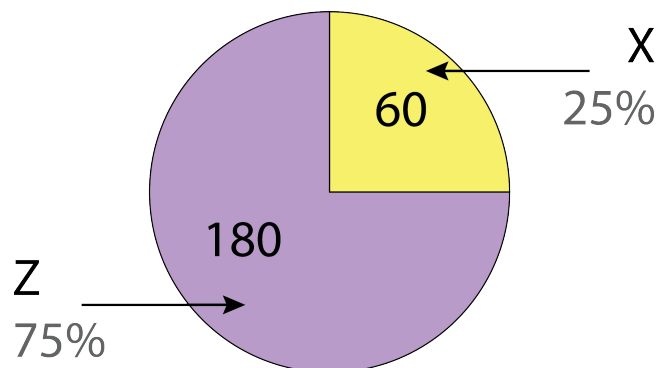
- If the circle chart values are 180 and 60, then the remaining three values would be the bar chart values. This would mean that the tallest bar would be representing the value 120 and the leftmost bar would be representing the value 40. This means the rightmost bar would be representing the remaining value, which is 30. Since the rightmost bar is more than half the height of the leftmost bar, the values of 40 and 30 would be reasonable.

Based on this logic, the leftmost bar represents the value 40. The top of the bar matches the second grid line. Since the grid lines are equally spaced, we can conclude that the distance between grid lines is  $40 \div 2 = 20$ .

Here is the labelled bar chart:



Here is the labelled circle chart:





## Problème de la semaine

### Problème A

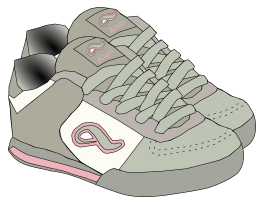
#### Horaire du gymnase

À l'école publique de Spruce Glen, chaque jour est divisé en neuf blocs. Chaque bloc a une durée de 30 minutes. Il y a six classes qui partagent le gymnase selon l'horaire hebdomadaire ci-dessous.

	Lundi	Mardi	Mercredi	Jeudi	Vendredi
<b>Bloc A</b>	Classe 1	Classe 3	Classe 2	Classe 3	Classe 6
<b>Bloc B</b>	Classe 5	Classe 5	Classe 2	Classe 3	Classe 1
<b>Bloc C</b>	Classe 3	Classe 5	Classe 2	Classe 2	Classe 3
<b>Bloc D</b>	Classe 3	Classe 5	Classe 5	Classe 2	Classe 3
<b>Bloc E</b>	Classe 6	Classe 1	Classe 5	Classe 6	Classe 3
<b>Bloc F</b>	Classe 4	Classe 2	Classe 6	Classe 1	Classe 5
<b>Bloc G</b>	Classe 4	Classe 6	Classe 1	Classe 1	Classe 2
<b>Bloc H</b>	Classe 2	Classe 4	Classe 3	Classe 4	Classe 2
<b>Bloc I</b>	Classe 2	Classe 4	Classe 4	Classe 5	Classe 4

- (a) À l'aide d'un diagramme à bandes, représente le temps total par semaine que consacre chaque classe à faire du sport au gymnase.
- (b) Classe, en ordre croissant, les classes selon le temps total par semaine qu'elles consacrent à faire du sport au gymnase.





## Problem of the Week

### Problem A and Solution

#### Gym Schedules

#### Problem

At Spruce Glen Public School, each day is divided into nine blocks, which are each 30 minutes long. There are six classrooms that share the gym, according to the weekly schedule shown.

	Monday	Tuesday	Wednesday	Thursday	Friday
<b>Block A</b>	Room 1	Room 3	Room 2	Room 3	Room 6
<b>Block B</b>	Room 5	Room 5	Room 2	Room 3	Room 1
<b>Block C</b>	Room 3	Room 5	Room 2	Room 2	Room 3
<b>Block D</b>	Room 3	Room 5	Room 5	Room 2	Room 3
<b>Block E</b>	Room 6	Room 1	Room 5	Room 6	Room 3
<b>Block F</b>	Room 4	Room 2	Room 6	Room 1	Room 5
<b>Block G</b>	Room 4	Room 6	Room 1	Room 1	Room 2
<b>Block H</b>	Room 2	Room 4	Room 3	Room 4	Room 2
<b>Block I</b>	Room 2	Room 4	Room 4	Room 5	Room 4

- (a) Make a bar chart showing the total gym time per week for each room.
- (b) List the rooms in order from least to greatest total gym time per week.

#### Solution

- (a) One way to draw the bar chart is to calculate the total gym time for each room. Then we can use the total times to determine the height of each bar. Remember that each block is 30 minutes long.

For example, if we add up the gym times for Room 1 in minutes we get:

- Monday time: 30 minutes
- Tuesday time: 30 minutes
- Wednesday time: 30 minutes
- Thursday time:  $30 + 30 = 60$  minutes
- Friday time: 30 minutes

Total time for Room 1 is  $30 + 30 + 30 + 60 + 30 = 180$  minutes



We could do these calculations for each room to get:

Total time for Room 2 is  $60 + 30 + 90 + 60 + 60 = 300$  minutes

Total time for Room 3 is  $60 + 30 + 30 + 60 + 90 = 270$  minutes

Total time for Room 4 is  $60 + 60 + 30 + 30 + 30 = 210$  minutes

Total time for Room 5 is  $30 + 90 + 60 + 30 + 30 = 240$  minutes

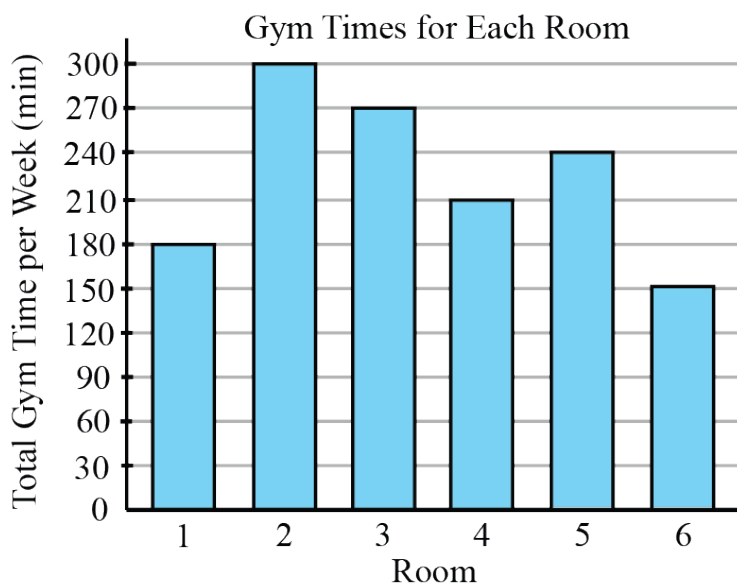
Total time for Room 6 is  $30 + 30 + 30 + 30 + 30 = 150$  minutes

Another way to build the bar chart is to count the total number of blocks that each class is in the gym. We can keep track of the number of blocks by using a tally chart.

Room	Number of Blocks
1	
2	
3	
4	
5	
6	

Then we can set our vertical axis to go up by 30 minute increments so that each tick mark in the bar chart represents one block in the gym.

The completed bar chart is shown.



(b) Looking at the size of the bars in the chart, the rooms in order from least to greatest total gym time per week is:

Room 6, Room 1, Room 4, Room 5, Room 3, Room 2






## Problème de la semaine


### Problème A

#### Les comptes à la confiserie

Ricardo et Nadia sont allés à la confiserie. Les indices ci-dessous décrivent les sortes et les quantités de bonbons qu'ils ont achetés.

- Ils ont acheté 8 paquets de Sunbursts.
- Ils ont acheté 4 paquets de Twinglers de plus que de paquets de Sunbursts.
- Ils ont acheté 6 paquets de Nerts de moins que de paquets de Twinglers.
- Ils ont acheté deux fois plus de paquets de W&Ws que de paquets de Nerts.
- Le nombre de paquets de Sweet Patch Kids est égal au nombre total de paquets de Sunbursts et de Nerts.
- Le nombre de paquets de Jolly Farmers est égal au nombre de paquets de Sweet Patch Kids moins le nombre de paquets de Twinglers.

Complète le pictogramme afin de représenter le nombre de paquets de chaque sorte de bonbons qu'ils ont acheté. Utilise un  pour représenter deux paquets de bonbons. À titre d'exemple, la première ligne a déjà été remplie.

Sorte de bonbons	Nombre de paquets
Sunbursts	
Twinglers	
Nerts	
W&Ws	
Sweet Patch Kids	
Jolly Farmers	

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# Problem of the Week

## Problem A and Solution


### Candy Store Counting





#### Problem

Ricardo and Nadia went to the candy store. The clues below describe the types and amount of candies they bought.

- They bought 8 packages of Sunbursts.
- They bought 4 more packages of Twinglers than Sunbursts.
- They bought 6 fewer packages of Nerts than Twinglers.
- They bought twice as many packages of W&Ws than Nerts.
- The number of packages of Sweet Patch Kids is equal to the total number of packages of Sunbursts and Nerts.
- The number of packages of Jolly Farmers is equal to the number of packages of Sweet Patch Kids minus the number of packages of Twinglers.

Complete the pictograph to show how many packages of each type of candy they purchased.

Use one  to represent two packages of candy. The first row has already been completed for you.

Type of Candy	Number of Packages
Sunbursts	   
Twinglers	
Nerts	
W&Ws	
Sweet Patch Kids	
Jolly Farmers	



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## Solution

First we need to calculate how many packages of each kind of candy they bought. We know they bought 8 packages of Sunbursts.

- Buying 4 more packages of Twinglers than Sunbursts means they bought  $8 + 4 = 12$  packages of Twinglers.
- Buying 6 fewer packages of Nerts than Twinglers means they bought  $12 - 6 = 6$  packages of Nerts.
- Buying twice as many packages of W&Ws than Nerts means they bought  $6 \times 2 = 12$  packages of W&Ws.
- The number of packages of Sweet Patch Kids they bought is  $8 + 6 = 14$ .
- The number of packages of Jolly Farmers they bought is  $14 - 12 = 2$ .

To complete the pictograph, we use  to represent two packages of candy. So we divide the number of packages for each type of candy by 2, in order to calculate the number of  needed for that candy in the pictograph.

The completed pictograph is shown below.

Type of Candy	Number of Packages
Sunbursts	   
Twinglers	     
Nerts	  
W&Ws	     
Sweet Patch Kids	      
Jolly Farmers	

**Key:** one  represents 2 packages of candy.

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# Raisonnement informatiques (C)

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## Problème de la semaine

### Problème A

#### Quel nombre suis-je?

Je suis un nombre de cinq chiffres composé des chiffres 0, 3, 4, 6 et 9 tel que:

- Le chiffre **4** occupe une position dont la valeur est 10 fois celle de la position occupée par le chiffre **9** et 100 fois celle de la position occupée par le chiffre **0**.
- Le chiffre **3** occupe une position dont la valeur est 100 fois celle de la position occupée par le chiffre **9**.
- Le chiffre **0** occupe une position dont la valeur est 10 fois celle de la position occupée par le chiffre **6**.

Quel nombre suis-je?





## Problem of the Week

### Problem A and Solution

#### What Number Am I?

#### Problem

I am a five-digit number made of the digits 0, 3, 4, 6, and 9. In my number, the following are true.

- The digit **4** is in a position whose place value is 10 times the place value of the position of the digit **9** and 100 times the place value of the position of the digit **0**.
- The digit **3** is in a position whose place value is 100 times the place value of the position of the digit **9**.
- The digit **0** is in a position whose place value is 10 times the place value of the position of the digit **6**.

What number am I?

#### Solution

The positions in a five-digit number are: ones (units), tens, hundreds, thousands, and ten thousands.

Since the 4 is in a position whose place value is 10 and 100 times the place value of other positions, the 4 cannot be in the ones or tens position.

Since the 3 is in a position whose place value is 100 times the place value of another position, the 3 cannot be in the ones or tens position.

Since the 0 is in a position whose place value is 10 times the place value of another position, the 0 cannot be in the ones position.

So the ones position must contain either the 9 or the 6.

Let's assume that the 9 is in the ones position. Based on the first clue, the 4 must be in the tens position since  $10 \times 1 = 10$ . However, we have already stated that the 4 cannot be in the ones or tens position. So we cannot put the 9 in the ones position.

Therefore, we can conclude that the 6 is in the ones position. Based on the third clue, the 0 must be in the tens position since  $10 \times 1 = 10$ . Knowing that the 0 is in the tens position, we can use the first clue to conclude that the 4 must be in the thousands position, since  $100 \times 10 = 1000$ . Also, the 9 must be in the hundreds position, since  $10 \times 100 = 1000$ . Now the only position that is left, the ten thousands position, must contain the only digit left which is the 3. This is consistent with the second clue since  $100 \times 100 = 10\,000$ .

Therefore, the number must be 34906.



## Problème de la semaine

### Problème A

#### Clés pour décoder des messages secrets

Il existe plusieurs manières d'encoder des messages. Voici un message codé contenant uniquement des zéros et des uns.

0 0 0 1 1 0 0 1 0 1 1 0 1 1 1 0

Cette seule suite peut représenter de nombreux messages différents. Pour bien décoder le message, il te faut une clé. Ce que représente le message codé dépend bien évidemment de la clé que tu utilises pour le décoder.

Voici deux clés que l'on pourrait utiliser pour décoder le message:

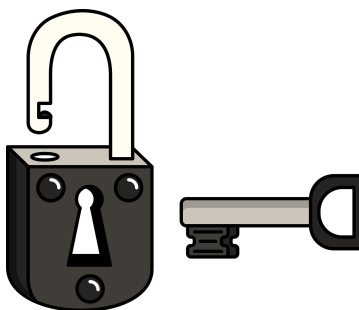
#### La clé Alpha

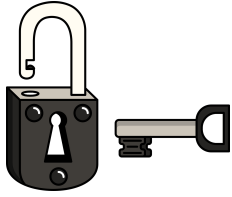
Lettre	Code
C	1 0 0
D	1 0 1 0
E	0 1
O	1 1 1
R	1 0 1 1
S	0 0
T	1 1 0

#### La clé Bêta

Lettre	Code
C	0 0 0 1
D	0 1 1 0
E	1 1 1 0
O	1 0 0 1
R	1 0 1 0
S	0 1 0 1
T	1 0 1 1

- (a) Quel message obtiens-tu si tu utilises la **clé Alpha** pour le décoder?  
(b) Quel message obtiens-tu si tu utilises la **clé Bêta** pour le décoder?





## Problem of the Week

### Problem A and Solution

### The Keys to Hidden Messages

#### Problem

There are many ways to encode messages. Here is an encoding using just zeros and ones.

0 0 0 1 1 0 0 1 0 1 1 0 1 1 1 0

This single sequence could represent many different messages. To decode the information correctly, you need a key. The actual message that the encoding represents depends on the key you use to decode it.

Here are two keys which could be used to decode the message:

Alpha Key	
Letter	Code
C	1 0 0
D	1 0 1 0
E	0 1
O	1 1 1
R	1 0 1 1
S	0 0
T	1 1 0

Beta Key	
Letter	Code
C	0 0 0 1
D	0 1 1 0
E	1 1 1 0
O	1 0 0 1
R	1 0 1 0
S	0 1 0 1
T	1 0 1 1

- (a) What is the message if you decode it using the **Alpha Key**?
- (b) What is the message if you decode it using the **Beta Key**?

#### Solution

We can use pattern matching to decode the message with each key.

- (a) The first row of the following table contains the message broken up into six pieces. Notice that each of these pieces is a code in the Alpha Key. The second row of the table contains the letter corresponding to each code.

0 0	0 1	1 0 0	1 0 1 1	0 1	1 1 0
S	E	C	R	E	T

Therefore, the message is “SECRET” when decoded using the Alpha Key.

- (b) The table below was created using a similar process as in part (a), except instead for the Beta Key.

0 0 0 1	1 0 0 1	0 1 1 0	1 1 1 0
C	O	D	E

Therefore, the message is “CODE” when decoded using the Beta Key.





## Problème de la semaine

### Problème A

#### Calculs de boîtes noires

Le CEMI a créé des boîtes noires qui transforment des nombres. Les machines acceptent un nombre comme entrée, effectuent des calculs sur ce nombre, puis produisent une sortie.

Ronit a configuré sa boîte noire pour qu'elle multiplie d'abord l'entrée par 2, puis qu'elle ajoute 8 à ce résultat.



Par exemple, si Ronit introduit le nombre 10 comme entrée, sa boîte noire multipliera d'abord ce nombre par 2 pour obtenir 20. Ensuite, elle ajoutera 8 à ce nombre pour produire une sortie finale de 28.

Amrita a configuré sa boîte noire pour qu'elle multiplie d'abord l'entrée par 4, puis qu'elle soustrait 6 de ce résultat.



- Si Amrita introduit le nombre 10 comme entrée, quel nombre la machine produira-t-elle comme sortie?
- Ronit et Amrita ont le même âge et ont plus de 3 ans. S'ils introduisent chacun leur âge comme entrée dans leur boîte noire, ils obtiennent tous deux la même sortie. Quel âge ont-ils ?
- Écris deux configurations de boîtes noires ayant 10 comme entrée et 16 comme sortie. Tu peux utiliser n'importe quelles deux opérations parmi les suivantes: addition, soustraction, multiplication ou division.



## Problem of the Week

### Problem A and Solution

#### Black Box Calculations

#### Problem

The CEMC has created black box machines that process numbers. The machines accept an input number, then do calculations based on that number, then produce an output.

Ronit set up his black box machine to first multiply the input number by 2, and then add 8 to the result.



For example, if Ronit inputs the number 10, his black box machine will first multiply it by 2 to produce the number 20. Then it will take the number 20 and add 8 to produce the final output of 28.

Amrita set up her black box machine to first multiply the input number by 4, and then subtract 6 from the result.



- Amrita inputs the number 10 into her black box machine. What number will the machine output?
- Ronit and Amrita are the same age and they are older than 3. They each put their age number into their black box machine and were surprised to get the same output as each other. How old are Ronit and Amrita?
- Write two black box machine setups that have an input of 10 and an output of 16. You can use any two of the following operations: addition, subtraction, multiplication, or division.

**Solution**

- (a) If Amrita inputs the number 10, the black box machine will first multiply it by 4 to produce the number 40. Then it will take the number 40 and subtract 6 to produce the final output of 34. So her black box machine will output 34.
- (b) One way to solve this problem is to create a table for each machine and keep track of the output produced for different inputs, starting at 4.

**Ronit's Machine**

Input	Result after multiplying by 2	Result after adding 8	Output
4	$4 \times 2 = 8$	$8 + 8 = 16$	16
5	$5 \times 2 = 10$	$10 + 8 = 18$	18
6	$6 \times 2 = 12$	$12 + 8 = 20$	20
7	$7 \times 2 = 14$	$14 + 8 = 22$	22

**Amrita's Machine**

Input	Result after multiplying by 4	Result after subtracting 6	Output
4	$4 \times 4 = 16$	$16 - 6 = 10$	10
5	$5 \times 4 = 20$	$20 - 6 = 14$	14
6	$6 \times 4 = 24$	$24 - 6 = 18$	18
7	$7 \times 4 = 28$	$28 - 6 = 22$	22

From these tables we see that when the input is 7, the output is 22 for both machines. So one possibility is that Ronit and Amrita are 7 years old.

Is it possible that Ronit and Amrita are a different age? Looking at the Output columns in the tables, we see that the output from Ronit's black box machine increases by 2 as the input increases by 1. However, the output from Amrita's black box machine increases by 4 as the input increases by 1. Since the output from Amrita's black box machine is increasing faster than the output from Ronit's black box machine, this tells us that their outputs will not be the same for any other possible ages.

So Ronit and Amrita must both be 7 years old.

- (c) There are many possible setups that would produce an output of 16 given an input of 10. Some setups are shown below.
- First divide by 5, then add 14.
  - First multiply by 2, then subtract 4.
  - First add 22, then divide by 2.
  - First subtract 2, then multiply by 2.

**EXTENSION:** We could describe the setup of each machine by writing a mathematical formula that describes the operations for the black box. The formula would use a letter such as  $n$  to represent the input number. Can you write a mathematical formula for each of the two machine setups from part (a)?



## Problème de la semaine

### Problème A

#### L'addition et la soustraction

Suis les étapes ci-dessous.

**Étape 1:** Choisis deux nombres différents de trois chiffres. Soit  $A$  le plus grand des deux nombres et  $B$  le plus petit.

**Étape 2:** Soustrais  $B$  de 999; soit  $C$  la différence obtenue.

**Étape 3:** Additionne  $A$  et  $C$ ; soit  $D$  la somme obtenue.

**Étape 4:** Soustrais 1000 de  $D$ ; soit  $E$  la différence obtenue.

**Étape 5:** Ajoute 1 à  $E$ ; soit  $F$  la somme obtenue.

- (a) Quel est le lien entre le nombre  $F$  et les nombres  $A$  et  $B$ ?
- (b) Essaie les mêmes étapes avec des nombres différents. Penses-tu que tu obtiendras toujours le même résultat? Explique pourquoi.





## Problem of the Week

### Problem A and Solution

### Adding and Subtracting

#### Problem

Follow the steps below.

**Step 1:** Pick two different three-digit numbers. Label the larger number  $A$  and the smaller number  $B$ .

**Step 2:** Subtract  $B$  from 999 and label the difference  $C$ .

**Step 3:** Add  $A$  and  $C$  and label the sum  $D$ .

**Step 4:** Subtract 1000 from  $D$  and label the difference  $E$ .

**Step 5:** Add 1 to  $E$  and label the sum  $F$ .

- What is the connection between the number  $F$  and the numbers  $A$  and  $B$ ?
- Try the same steps with different numbers. Do you think you will always get the same result? Why or why not?

#### Solution

- We can work through this procedure with any two, random, three-digit numbers. Let's try starting with 814 and 275.

**Step 1:** The larger number 814 is labelled  $A$ , and the smaller number 275 is labelled  $B$ .

**Step 2:** The difference  $999 - B$  is  $999 - 275 = 724$ , and is labelled  $C$ .

**Step 3:** The sum  $A + C$  is  $814 + 724 = 1538$ , and is labelled  $D$ .

**Step 4:** The difference  $D - 1000$  is  $1538 - 1000 = 538$ , and is labelled  $E$ .

**Step 5:** The sum  $E + 1$  is  $538 + 1 = 539$ , and is labelled  $F$ .

Notice that  $814 - 275 = 539$ . So  $A - B = F$ .

- If you try this procedure with any two three-digit numbers, it will always work out that  $A - B = F$ . We will show this using algebra.

**Step 1:** We choose three-digit numbers  $A$  and  $B$  so that  $A \geq B$ .

**Step 2:** We calculate  $999 - B$ , and label this  $C$ . That is,  $C = 999 - B$ .

**Step 3:** We add  $A + C$ . So, we calculate  $A + 999 - B$ , and label this  $D$ . That is,  $D = A + 999 - B$ .

**Step 4:** We subtract 1000 from  $D$ . So, we calculate  $A + 999 - B - 1000$ , and label this  $E$ . That is,  $E = A + 999 - B - 1000$ .

**Step 5:** We add 1 to  $E$ . So, we calculate  $A + 999 - B - 1000 + 1$ , and label this  $F$ . That is,  $F = A + 999 - B - 1000 + 1$ .

Now, we can simplify this expression to get  $A - B + 999 - 1000 + 1 = A - B$ , since  $999 - 1000 + 1 = 0$ . So,  $F = A - B$ .

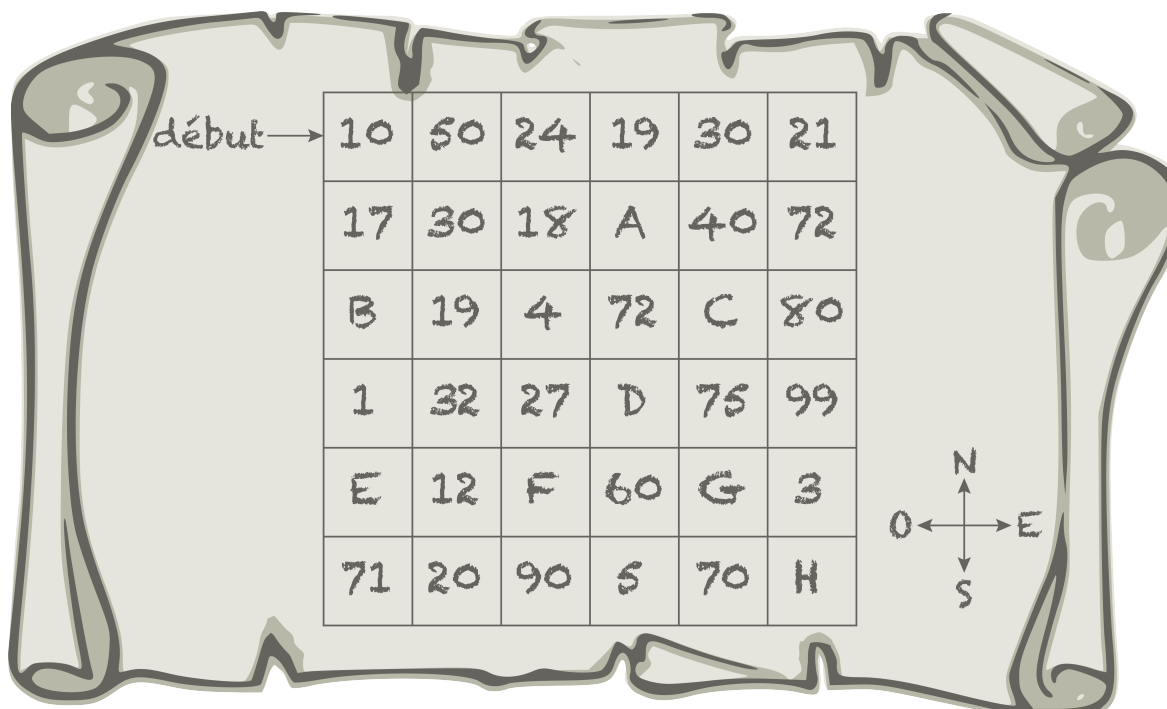


## Problème de la semaine

### Problème A

#### La carte au trésor

Robbie a trouvé une carte au trésor qui contient une grille remplie de nombres et de lettres.



La chasse au trésor commence dans le coin nord-ouest de la carte sur la case qui contient le nombre 10. Les cases contenant des nombres déterminent la direction à prendre selon les règles suivantes.

- Si le nombre est pair et un multiple de 5, déplace-toi d'une case vers l'est.
- Si le nombre est pair mais n'est pas un multiple de 5, déplace-toi d'une case vers le sud.
- Si le nombre est un multiple de 5 mais n'est pas pair, déplace-toi d'une case vers le nord.
- Si le nombre n'est ni pair ni un multiple de 5, déplace-toi d'une case vers l'ouest.

Les cases contenant des lettres représentent les emplacements possibles du trésor. Si Robbie suit les règles, il suivra un chemin qui le conduira à une case contenant une lettre. Cette case est l'endroit où est caché le trésor. À quel endroit le trésor est-il caché?

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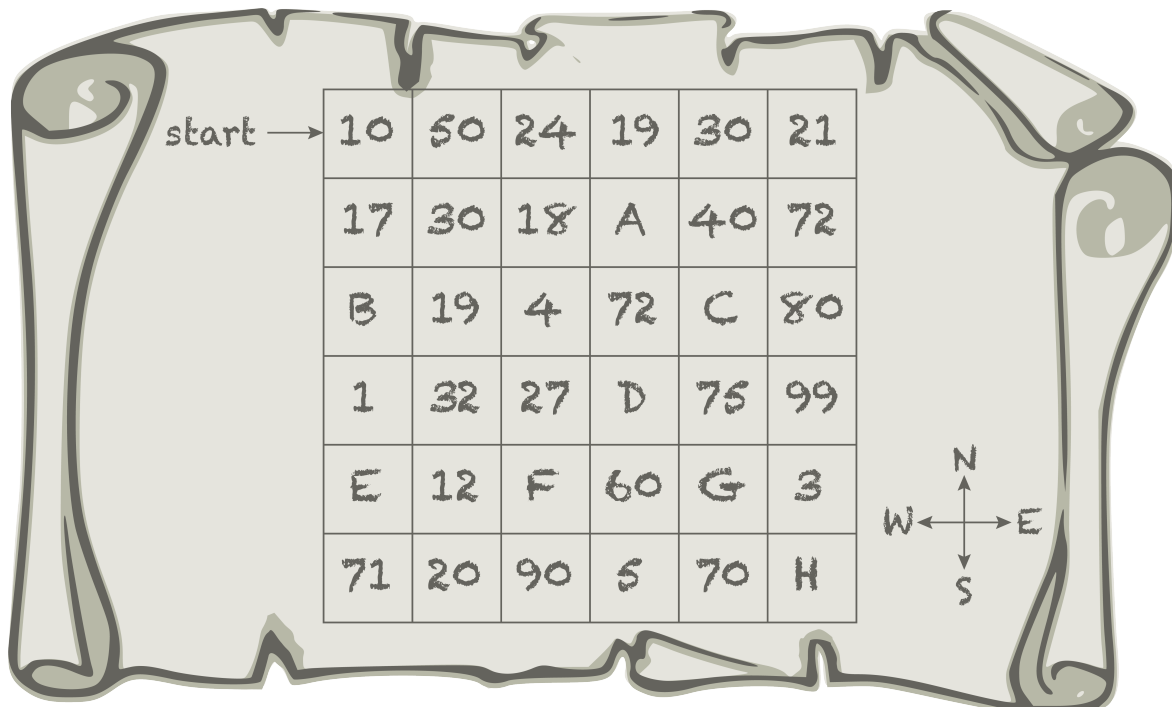
## Problem of the Week

### Problem A and Solution

#### Treasure Map

#### Problem

Robbie found a treasure map that contains a grid filled with numbers and letters.



The treasure hunt starts in the northwest corner of the grid, on the square that contains the number 10. The squares with numbers are used to determine which way to go, using the following rules.

- If the number is even and a multiple of 5, then move one square east.
- If the number is even, but not a multiple of 5, then move one square south.
- If the number is a multiple of 5, but not even, then move one square north.
- If the number is neither even nor a multiple of 5, then move one square west.

The squares with letters represent possible locations of the treasure. If Robbie follows the rules, he will follow a path that reaches a square with a letter, which is where the treasure is hidden. Where is the treasure hidden?

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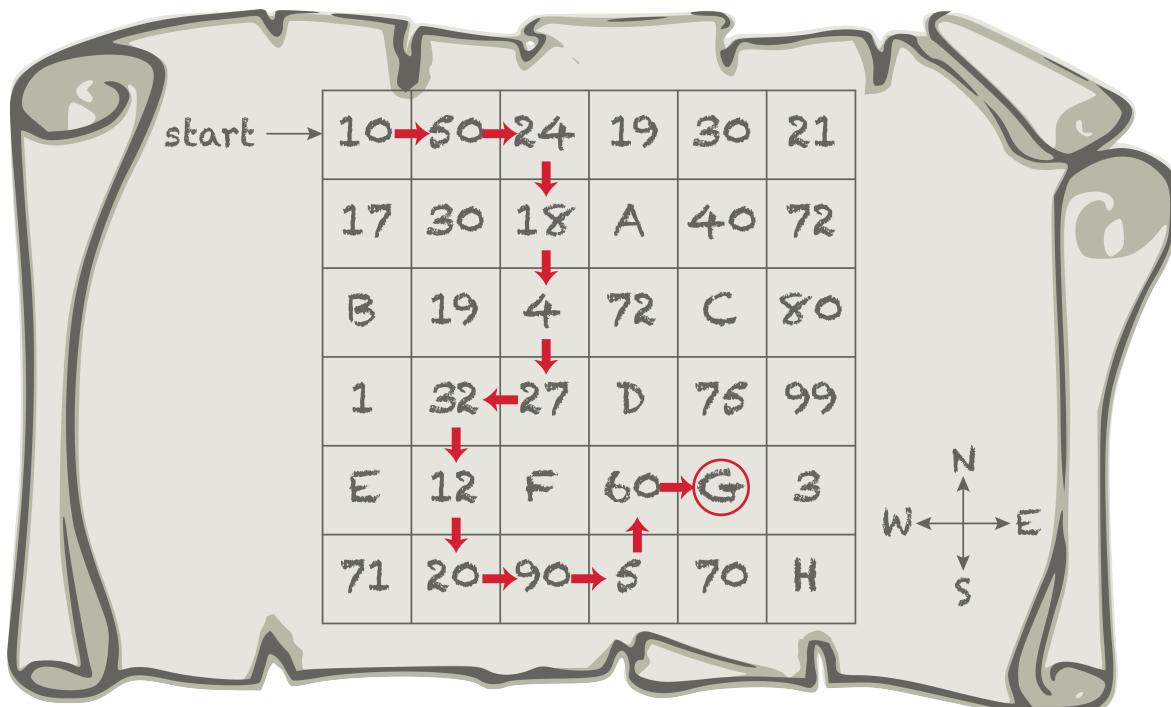


### Solution

Starting in the northwest corner of the map, here are the steps Robbie would follow to find the hidden treasure.

- 10 is an even number and a multiple of 5, so move one square east.
- 50 is an even number and a multiple of 5, so move one square east again.
- 24 is an even number but not a multiple of 5, so move one square south.
- 18 is an even number but not a multiple of 5, so move one square south again.
- 4 is an even number but not a multiple of 5, so move one square south again.
- 27 is neither even nor a multiple of 5, so move one square west.
- 32 is an even number but not a multiple of 5, so move one square south.
- 12 is an even number but not a multiple of 5, so move one square south again.
- 20 is an even number and a multiple of 5, so move one square east.
- 90 is an even number and a multiple of 5, so move one square east again.
- 5 is a multiple of 5 but not an even number, so move one square north.
- 60 is an even number and a multiple of 5, so move one square east.
- Robbie has reached a square with a letter, so the treasure is hidden in location G.

The path to the hidden treasure is shown on the map below.







## Problème de la semaine

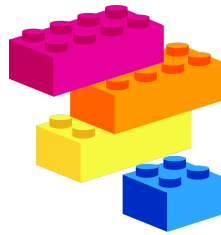
### Problème A

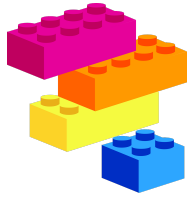
#### Récréation intérieure

Ce printemps a été très humide et pluvieux. Il a tellement plu que les élèves de l'Académie Rising Up n'ont pas pu aller dehors pour la récréation pendant toute une semaine, du lundi au vendredi. À la place, les élèves ont choisi parmi les activités intérieures suivantes: jeu d'association, Pictionary, dames, blocs de construction et origami. Carlo a choisi une activité différente chaque jour.

À l'aide des indices suivants, détermine quelle activité Carlo a choisi chaque jour.

- (1) Mardi ou vendredi, Carlo a joué avec les blocs de construction.
- (2) Carlo a fait de l'origami la veille du jour où il a joué au jeu d'association.
- (3) Jeudi, Carlo n'a pas joué à Pictionary.
- (4) Carlo a joué au jeu d'association deux jours avant de jouer aux dames.





## Problem of the Week

### Problem A and Solution

#### Indoor Recess

#### Problem

It has been a wet spring so far. It has rained so much that the students at Rising Up Academy were not able to go outside for recess for a whole week, from Monday to Friday. Instead the students chose from the following indoor activities: matching game, Pictionary, checkers, building blocks, and origami. Carlo did a different indoor activity each day.

Using the following clues, determine which indoor activity Carlo did each day.

- (1) On either Tuesday or Friday Carlo played with the building blocks.
- (2) Carlo did origami the day before he played the matching game.
- (3) On Thursday Carlo did not play Pictionary.
- (4) Carlo played the matching game two days before he played checkers.

#### Solution

From clue (2), we know Carlo did origami the day before he played the matching game. From clue (4), we know Carlo played the matching game two days before he played checkers. So, putting these clues together tells us that we have two possibilities. One possibility is that Carlo did origami on Tuesday, played the matching game on Wednesday, and played checkers on Friday. Another possibility is that Carlo did origami on Monday, played the matching game on Tuesday, and played checkers on Thursday. Let's look at each of these possibilities.

- Suppose Carlo did origami on Tuesday, played the matching game on Wednesday, and played checkers on Friday. Then he must have played Pictionary and played with the building blocks on Monday and Thursday, in some order. However, from clue (3) we know that Carlo did not play Pictionary on Thursday and from clue (1) we know that Carlo did not play with the building blocks on Thursday. Therefore this possibility won't work.
- Suppose Carlo did origami on Monday, played the matching game on Tuesday, and played checkers on Thursday. Then he must have played Pictionary and played with the building blocks on Wednesday and Friday, in some order. We know from clue (1) that Carlo did not play with the building blocks on Wednesday. That means he must have played with the building blocks on Friday, and played Pictionary on Wednesday. We can verify that this order satisfies all four clues given in the problem.

Therefore, Carlo did origami on Monday, played the matching game on Tuesday, played Pictionary on Wednesday, played checkers on Thursday, and played with the building blocks on Friday.